



## Spectral Broadening induced by XPM in HNLF

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## **Photonic Firewall**



**Photonic firewall:** It leverages the all-optical pattern matching to directly identify the signals in the optical domain. It can distinguish hidden network intrusions and attacks, and finally selects corresponding defense means according to the set security policy.







#### **Compositions of Photonic Firewall**



The key optical parts of the system are an XNOR gate and a recirculating AND gate loop. In project WISDOM, both are separately demonstrated at 42.6 Gbps using hybrid-integrated SOA-MZIs.





## **Logic Gates achieved with HNLF**



Pantelis Velanas, Adonis Bogris, Dimitris Syvridis, "Operation properties of a reconfigurable photonic logic gate based on cross phase modulation in highly nonlinear fibers," *Opt. Fiber Technol.*, vol. 15, no. 1, pp. 65–73, Jan. 2009.



## **Fiber Nonlinearities**



The response of any dielectric to light becomes nonlinear for intense electromagnetic fields, and optical fibers are no exception. As a result, the total polarization **P** induced by electric dipoles is not linear in the electric field **E**, but satisfies the more general relation

$$P = \varepsilon_0 \left( \chi^{(1)} \cdot E + \chi^{(2)} : EE + \chi^{(3)} : EE + \cdots \right)$$

Where  $\varepsilon_0$  is the vacuum permittivity and  $\chi^{(j)}$  is *j*th order susceptibility. In general,  $\chi^{(j)}$  is a tensor of rank j + 1.

**Cross-phase modulation (XPM)**: It refers to the nonlinear phase shift of an optical field induced by another field having a different wavelength, direction, or state of polarization.

$$\phi_{NL} = n_2 k_0 L(|E_1|^2 + 2|E_2|^2)$$

$$\uparrow \qquad \uparrow$$

$$SPM \qquad XPM$$



#### **Spectral Effects**



Considering the spectral change occurring as a result of XPM interaction between two co-propagating pulses with non-overlapping spectra.

$$\frac{\partial A_1}{\partial z} + \frac{i\beta_{21}}{2} \frac{\partial^2 A_1}{\partial T^2} = i\gamma_1 (|A_1|^2 + 2|A_2|^2) A_1$$
$$\frac{\partial A_2}{\partial z} + d \frac{\partial A_2}{\partial T} + \frac{i\beta_{22}}{2} \frac{\partial^2 A_2}{\partial T^2} = i\gamma_2 (|A_2|^2 + 2|A_1|^2) A_2$$

where

$$T = t - \frac{z}{v_{g1}}, \quad d = \frac{v_{g1} - v_{g2}}{v_{g1}v_{g2}}$$

 $A_j$  is the slowly varying amplitude. Time T is measured in a reference frame moving with the pulse traveling at speed  $v_{g1}$ . The parameter *d* is a measure of group-velocity mismatch between the two pulses.



#### **Spectral Effects**



Using the width  $T_0$  of the first pulse at the wavelength  $\lambda_1$  as a reference, the walk-off length  $L_W$  and the dispersion length  $L_D$  are induced as

$$L_W = T_0 / |d|$$
,  $L_D = T_0^2 / |\beta_{21}|$ 

**Case 1:** Fiber length  $L \ll L_D$  and  $L \ll L_W$ , the dispersive effects can be neglected.

**Case 2:** Fiber length  $L \ll L_D$  and  $L \gg L_W$ , even though pulse shape does not change, the spectrum is affected drastically.

**Case 3:** Fiber length  $L > L_D$  and  $L > L_W$ , XPM can affect both the pulse shape and the spectrum.





Consider the simple case  $L \ll L_D$  and  $L > L_W$ , as the pulse shapes do not change in the absence of GVD,  $A_j$  can be solved analytically. The general solution at z = L is given by

 $A_1(L,T) = A_1(0,T)e^{i\phi_1}, \quad A_2(L,T) = A_2(0,T-dL)e^{i\phi_2}$ 

where the nonlinear phase shifts are time-dependent.

As an illustration, consider the case of two unchirped Gaussian pulses of the same width  $T_0$  with the initial amplitudes

$$A_1(0,T) = \sqrt{P_1} \exp\left(-\frac{T^2}{2T_0^2}\right), \quad A_2(0,T) = \sqrt{P_2} \exp\left(-\frac{(T-T_d)^2}{2T_0^2}\right)$$

where  $P_1$  and  $P_2$  are the peak powers and  $T_d$  is the initial time delay between the two pulses.





Thus, the time-dependent nonlinear phase shifts are obtained from

$$\phi_j(\tau) = \gamma_j L\left(P_j e^{-\tau^2} + P_{3-j} \frac{\sqrt{\pi}}{\delta} |erf(\tau - \tau_d) - erf(\tau - \tau_d - \delta)|\right)$$

where *erf*(*x*) stands for the error function and



Spectral of two pulses exhibiting XPM-induced asymmetric spectral broadening. The parameters are  $\gamma_1 P_1 L=40$ ,  $P_2/P_1=0.5$ ,  $\gamma 2/\gamma 1=1.2$ ,  $\tau_d=0$ , and  $L/L_W=5$ .





A qualitative understanding of the spectral features can be developed from the XPM-induced frequency chirp using

$$\Delta v_j(\tau) = -\frac{1}{2\pi} \frac{\partial \phi_j}{\partial T} = \frac{\gamma_j L}{\pi T_0} \left[ P_j \tau e^{-\tau^2} - \frac{P_{3-j}}{\delta} \left( e^{-(\tau - \tau_d)^2} - e^{-(\tau - \tau_d - \delta)^2} \right) \right]$$

We consider the pump–probe configuration assuming  $P_1 \ll P_2$ . The pump-induced chirp imposed on the probe pulse can be obtained by neglecting the SPM contribution and is of the form

$$\Delta v_1(\tau) = -\operatorname{sgn}(\delta) \Delta v_{\max} \exp[-(\tau - \tau_d)^2] - \exp[-(\tau - \tau_d - \delta)^2]$$

Where  $\Delta v_{max}$  is the maximum XPM-induced chirp given by

$$\Delta v_{\max} = \frac{\gamma_1 P_2 L}{\pi T_0 |\delta|} = \frac{\gamma_1 P_2 L_W}{\pi T_0}$$







For  $\tau_d = 0$ , the probe spectrum is shifted toward blue with strong asymmetry.

For  $\tau_d$  = 2, the probe becomes spectrum symmetric.

For  $\tau_d = 4$ , the probe spectrum is again asymmetric with a shift toward red.

Probe spectrum together with phase and chirp for  $\delta = -4$  and  $\tau_d = 0$ , 2, and 4.

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#### **Simulations Setup**



Design setup of spectral broadening induced by XPM

The fiber length L = 93.5 km, nonlinearity coefficient  $\gamma$  = 34 W<sup>-1</sup>·km<sup>-1</sup>, chromatic dispersion of 16 ps/nm·km at 193.1 THz, and dispersion slope of 0.08 ps/nm<sup>2</sup>·km.



#### Results





The leading edge of pump pulse interacts with the probe pulse, therefore the XPM-induced chirp is negative and the spectrum is shifted toward red.



#### Results





The probe pulse interacts with the trailing edge of the pump pulse. As a result, the XPM-induced chirp is positive and the probe spectrum starts to shift toward blue.





## **Conclusions & future works**

#### **Conclusions:**

- Different from the case of pure SPM, the XPM-induced spectral broadening is usually asymmetric.
- □ The output spectrum of probe pulse depends on the chirp it experienced.

#### **Future works:**

- Realize a similar probe spectrum when the pulse width reduces, so that the logic gates with higher data rate can be achieved.
- Apply the constructed photonic logic gates to the architecture of WISDOM project.





# Thank you for your attention!

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