

Flexible Architectures for Next-Generation Optical Networks

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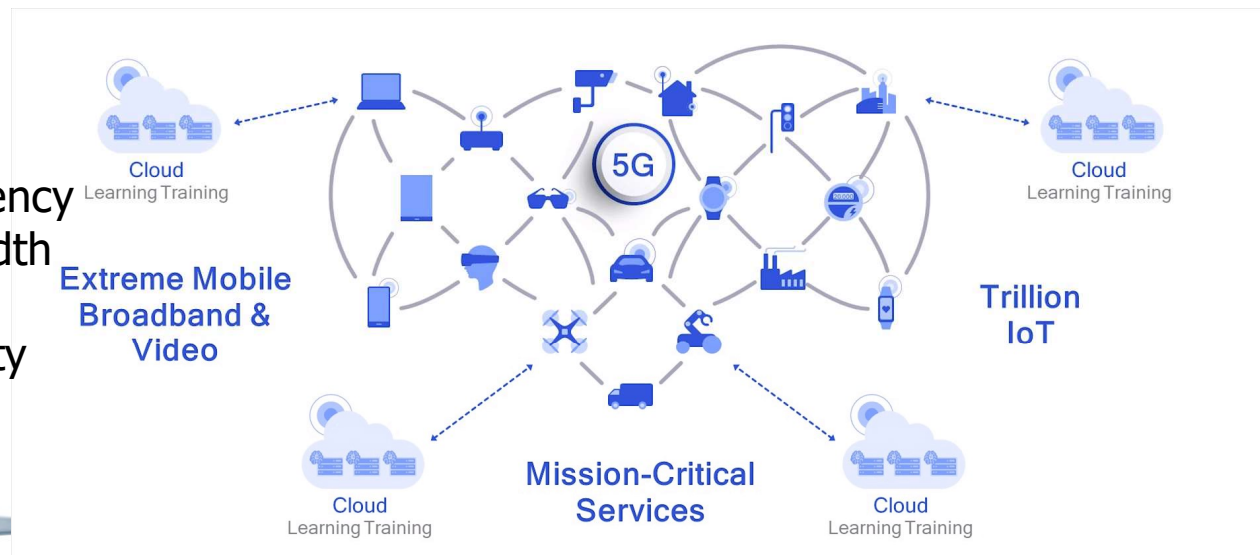
Outline

- **Introduction**
- Contribution I: High-precision time synchronization techniques for optical datacenter networks and a zero-overhead microsecond-accuracy solution
- Contribution II: Dynamic routing, spectrum, and modulation format assignment in co-existing fixed/flex-grid optical networks
- Contribution II: Cost-efficient C+L Bands Upgrade Strategies to Sustain Long-term Traffic Growth.
- Conclusion and future research ideas

Flexible Network Architectures

A flexible network solution enables customization of network operations according to the changing network demand

- ✓ Ultra low-latency
- ✓ High bandwidth availability
- ✓ Ultra reliability



Source: <https://www.techspot.com/article/1582-state-of-5g-wireless/>

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- Conclusion and future research ideas

Agenda

- ✓ Introduction to the problem
- ✓ Proposed solution
 - *PTP time synchronization in an optical datacenter network with zero-overhead transmission and microsecond-accuracy*
- ✓ Results
- ✓ Summary and future work

Time Synchronization

Coordinating independent clocks running on different machines with a standard time

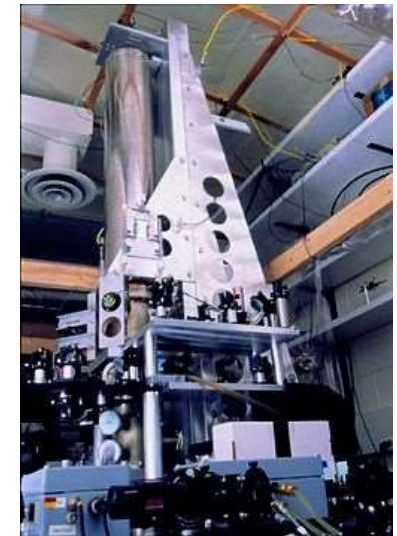
Atomic Clocks

- Use resonance frequencies of atoms

Global Navigation Satellite Systems:

- Periodically synchronize to atomic clocks

Oscillator Type	Accuracy	Cost
Quartz crystal	10^{-5} to 10^{-4}	Inexpensive
Rubidium	10^{-9}	\$800 USD
Cesium	10^{-13} to 10^{-12}	\$50000 USD

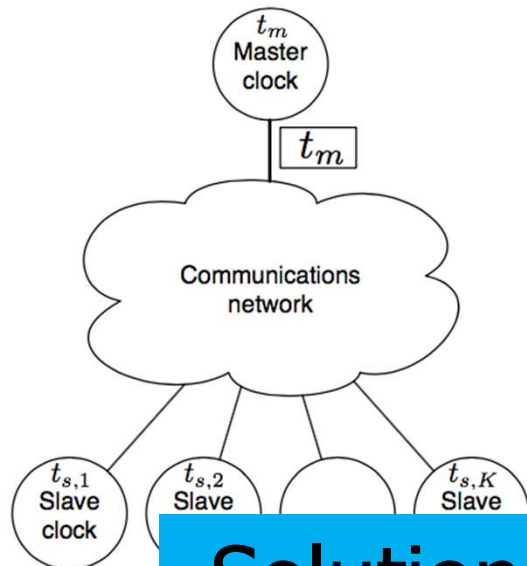


Atomic Clock, Boulder, CO, USA

Source: <https://en.wikipedia.org/wiki/NIST-F1>

Time Synchronization: Distributed Systems

Multiple clocks in a distributed system needs to maintain same global time!



$$t_{s,k} = t_m + \theta$$

$t_{s,k}$: time at slave clock k

t_m : time at master node

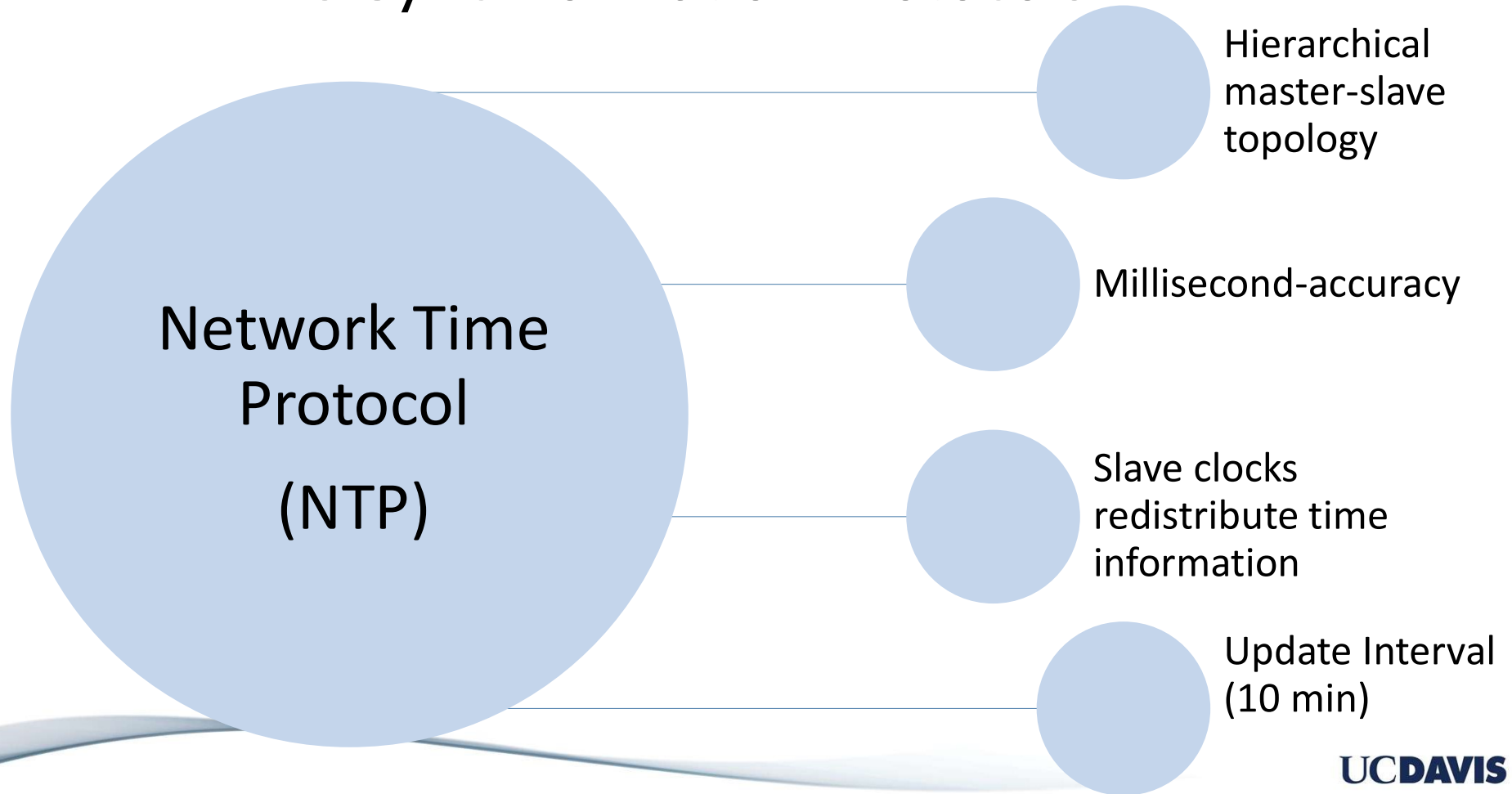
θ : offset due to environmental effect

$$t_{s,k} = t_m + \theta + d$$

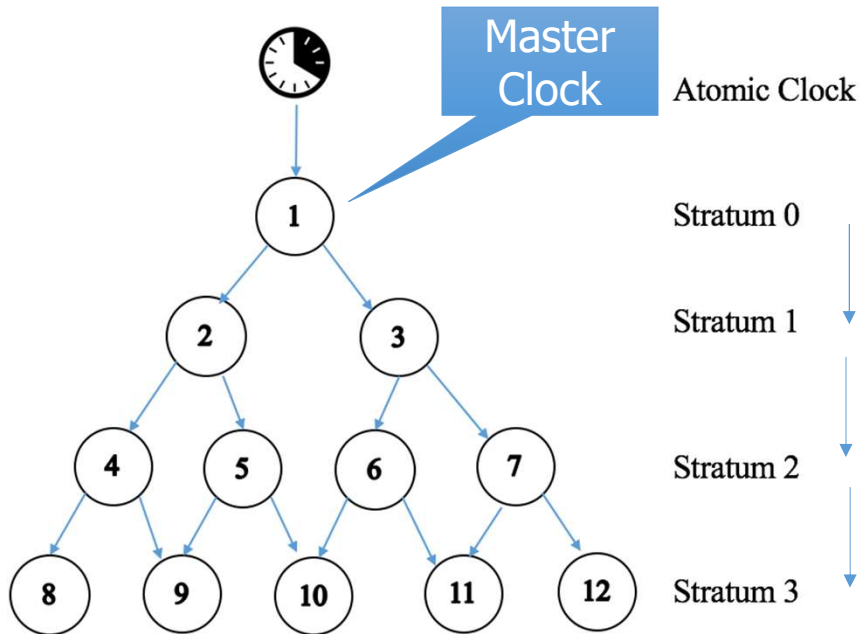
d : average delay between master and slave nodes

Solution is to find this offset and delay

Time Synchronization Protocols: NTP



Time Synchronization Protocols: NTP



Stratum denotes distance from the master clock

Delay, d_1

Delay, $d_2 = d_1 + d_2$

Delay, $d_3 = d_1 + d_2 + d_3$

- Queueing delay
- Processing delay
- Routing path
- Cable length



NTP master clock

Source: https://www.worldtimesolutions.com/products/ntp_server.html

Time Synchronization Protocols: PTP

Precision Time Protocol



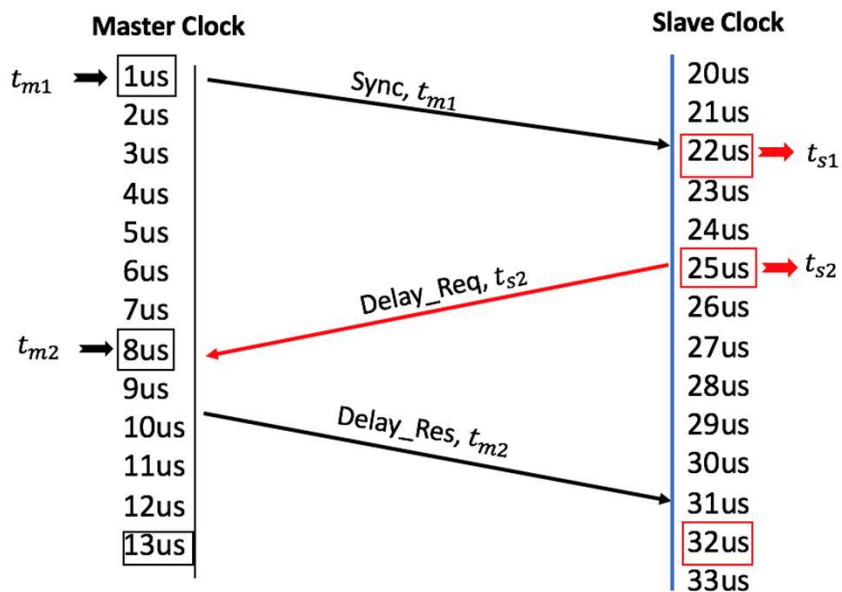
Hierarchical master-slave topology

Microsecond/nanosecond-accuracy

Slave clocks **does not** redistribute time information

Update interval (1 sec)

Time Synchronization Protocols: PTP

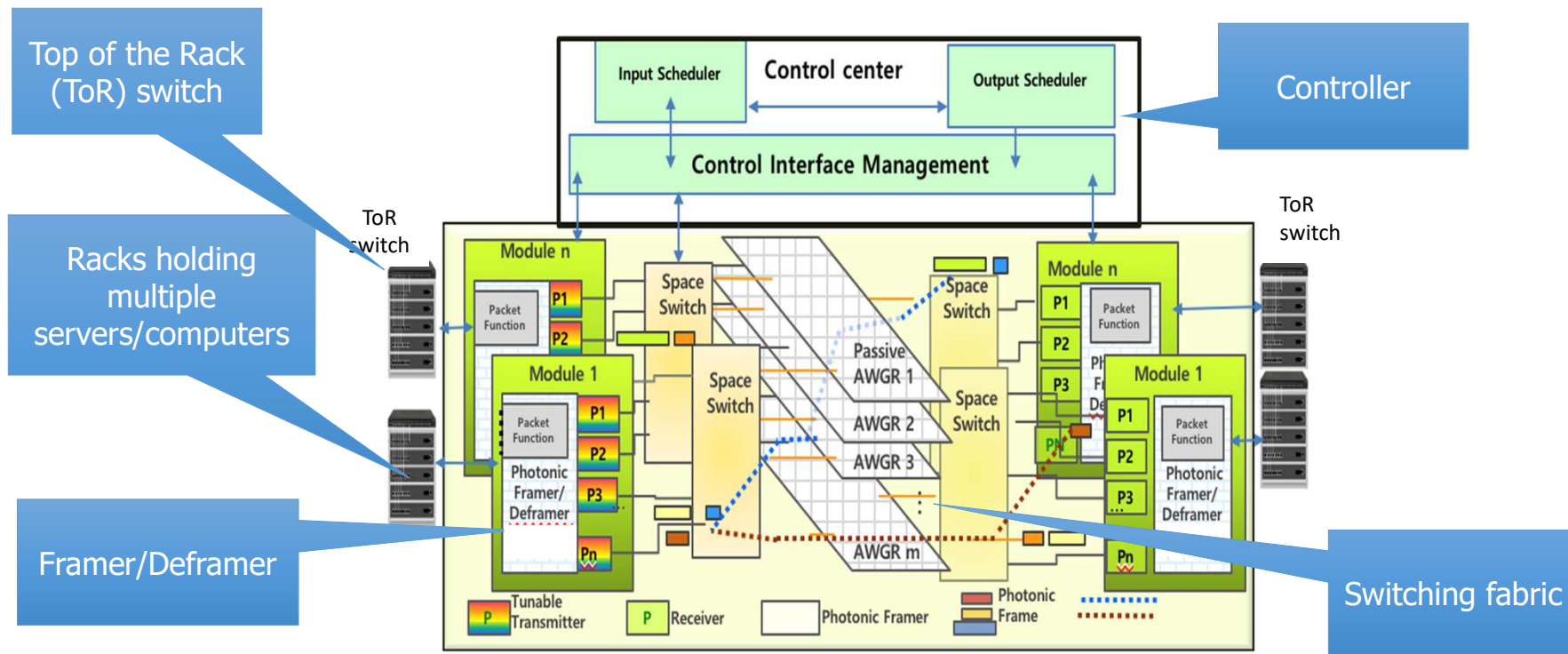


$$\begin{aligned} \text{Avg path delay} &= \frac{(t_{s1} - t_{m1}) + (t_{m2} - t_{s2})}{2} \\ &= \frac{(22 - 1) + (8 - 25)}{2} = 2 \text{ us} \end{aligned}$$

$$\begin{aligned} \text{Time offset} &= t_{s1} - t_{m1} - \text{Avg path delay} \\ &= 22 - 1 - 2 = 19 \text{ us} \end{aligned}$$

$$\text{Slave clock time} = 32 - 19 = 13 \text{ us}$$

Packet Switched Optical Datacenter Network (PSON)



Problem Statement

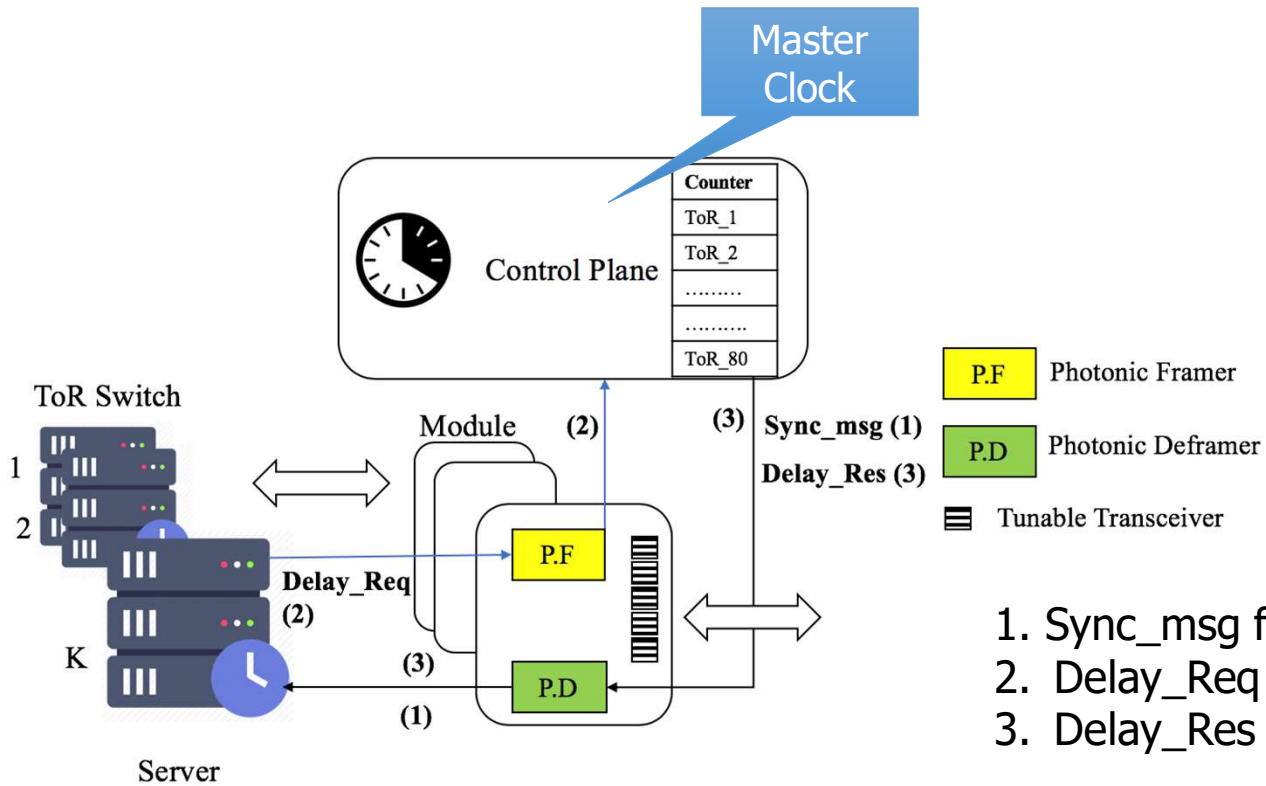
- Given:
 - PSON datacenter Architecture
 - Three traffic distributions: Lognormal, Pareto, Uniform
 - PTP enabled ToR switches
 - Controller with atomic/GPS clock information
- Objective:
 - *Synchronize ToR switches in a PSON with microsecond accuracy.*

Proposed Algorithm

Algorithm 1 PTP Time Synchronization Through In-Band Transmission

- 1: **Input:** packet size, traffic load, link bandwidth of datacenter, number of ToR switches, resynchronization-interval time;
- 2: **Output:** Time error;
- 3: Initialize counter times for all ToR switches (limit time at resynchronization-interval time);
- 4: Create a list of candidate ToR switches which have counter time equal to resynchronization-interval time (that means this ToR switch needs to be synchronized);
- 5: **if** ToR switch ϵ candidate list **then**
 - 6: wait_sync_time \leftarrow wait time for data packets in deframer to send 'sync' message to
 - 7: candidate ToR switches with packets generated from a specific traffic distribution;
 - 8: wait_delay_req_time \leftarrow wait time for data packets in framer to send 'delay request'
 - 9: message to controller with packets generated from the same traffic distribution;
 - 10: counter time of that ToR \leftarrow zero;
 - 11: Time error \leftarrow wait_sync_time + wait_delay_req_time;
 - 12: Candidate list \leftarrow candidate list synced TOR;
- 13: **else**
 - 14: counter time of that ToR \leftarrow counter time++;
- 15: **end if**
- 16: Repeat from Step 4;

Proposed Method



PTP master clock

Source:

<https://www.cisco.com/c/en/us/support/switches/nexus-3064-switch/model.html>

1. Sync_msg from controller to ToR switch
2. Delay_Req msg from ToR switch to controller
3. Delay_Res msg from controller to ToR switch

Simulation setup

- Number of ToR Switch: 80
- Number of Framer/deframer: 80
- Maximum length of PTP message: ~300 bits
- Data packet length: 200 to 1400 bytes
- Re-synchronization interval: 1 second

Performance Evaluation Metric

$$Time - error = Sync_msg_{wait} + Delay_req_{wait} + Delay_res_{wait}$$

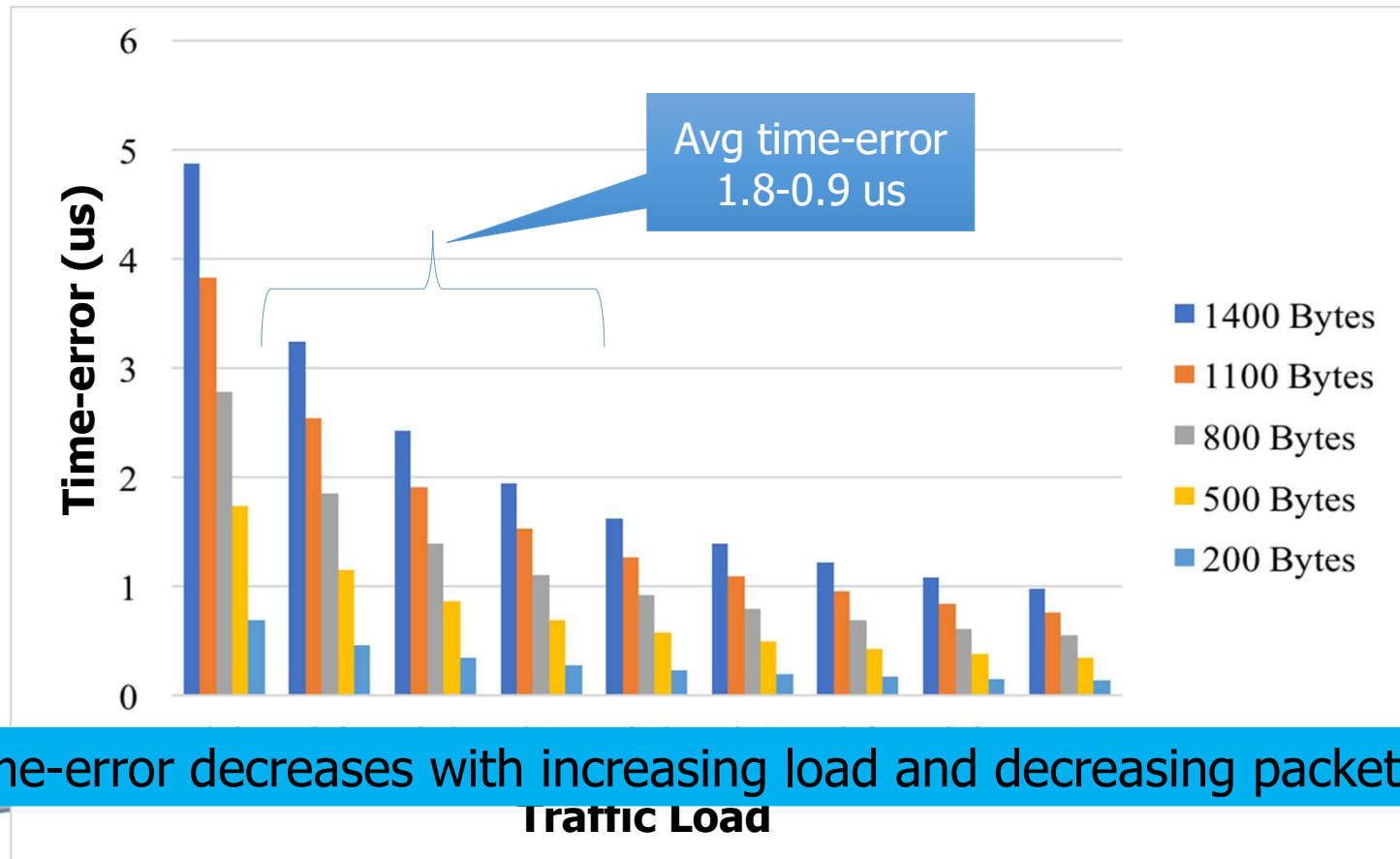
$Sync_msg_{wait}$
= wait time for data packets in deframer to send '**Sync**' message to ToR switches

$Delay_req_{wait}$ = for data packets in framer to send '**Delay request**', message to controller

$Delay_res_{wait}$ = for data packets in deframer to send '**Delay response**', message to ToR switches

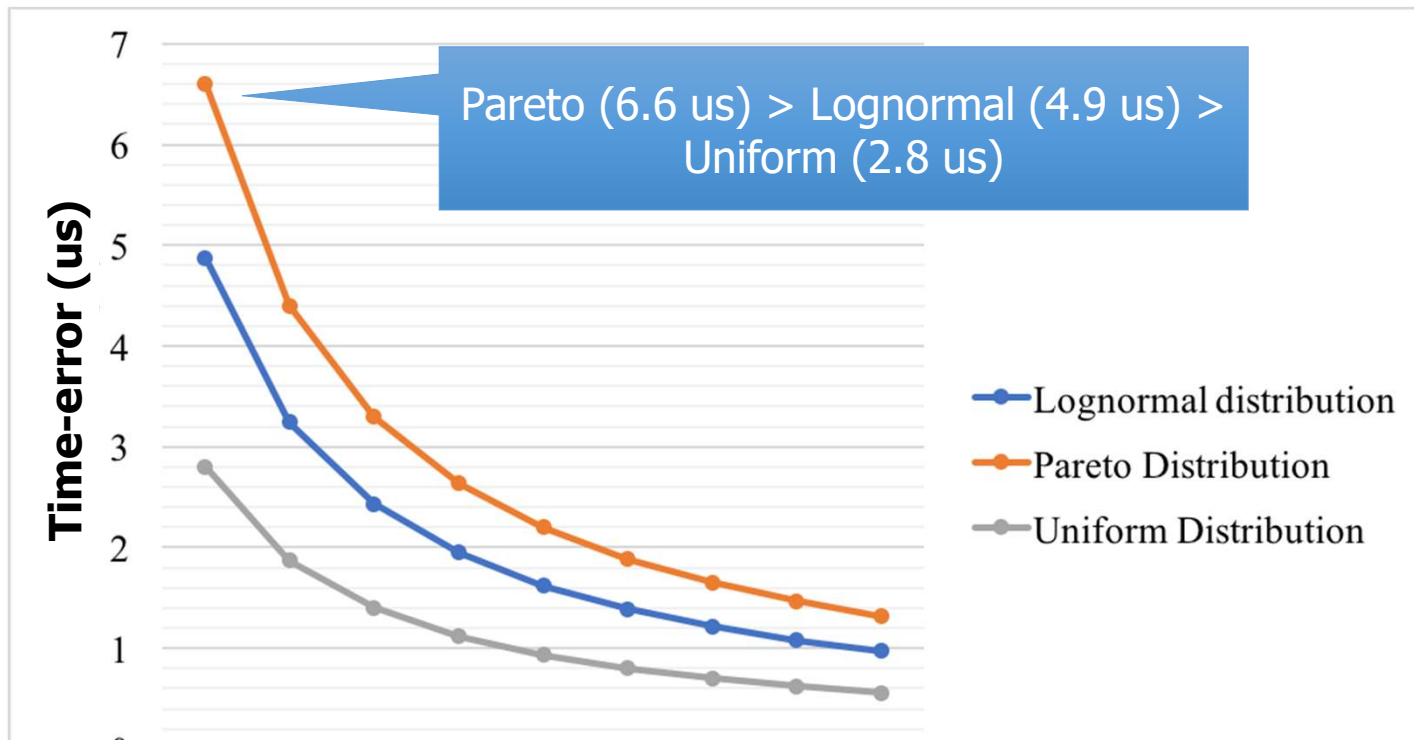
- Traffic load
- Packet-length
- Traffic distribution

Results: Time-error vs. Load (Lognormal)



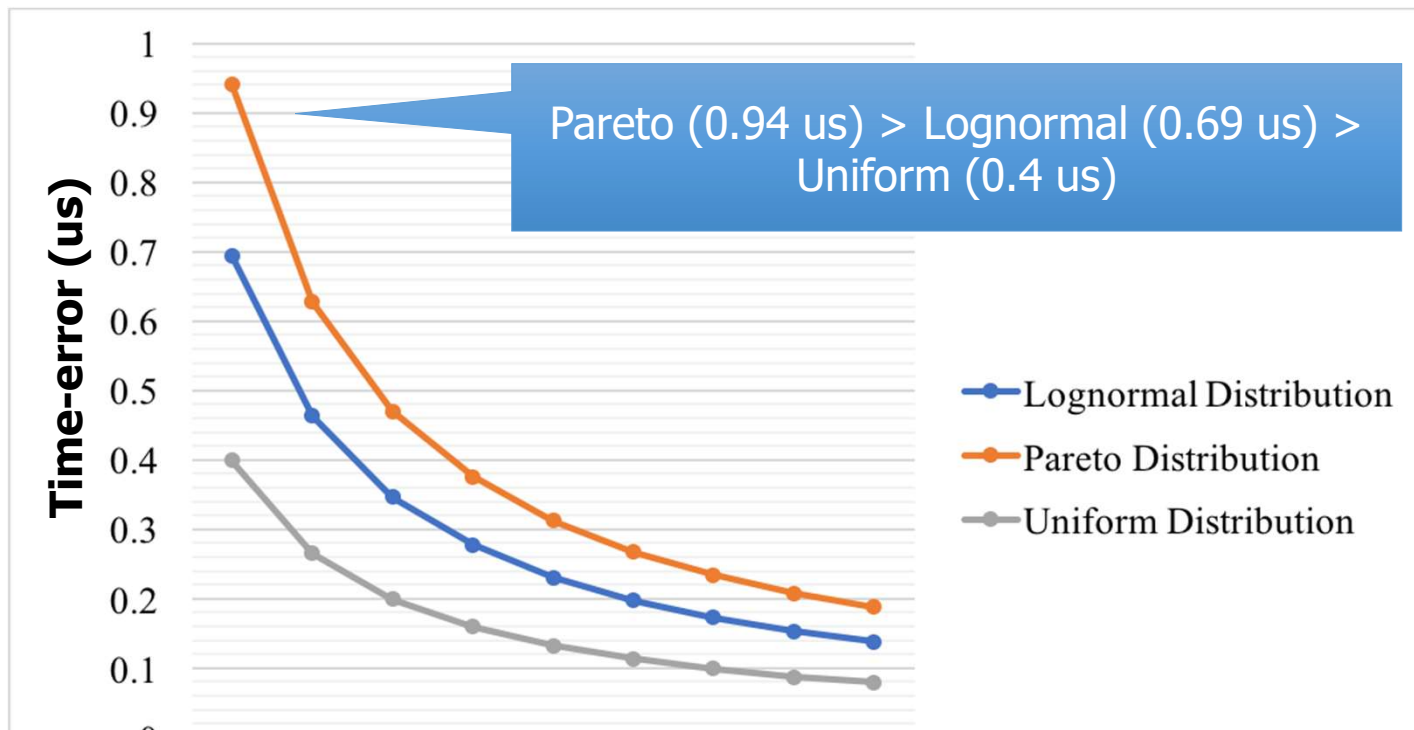
Time-error decreases with increasing load and decreasing packet-length

Results: Time-error vs. Load (1400 bytes)



Time-error is the highest for packet length of 1400 bytes. Pareto distribution obtains highest time-error among others

Results: Time-error vs. Load (200 bytes)



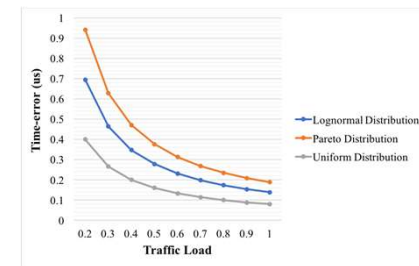
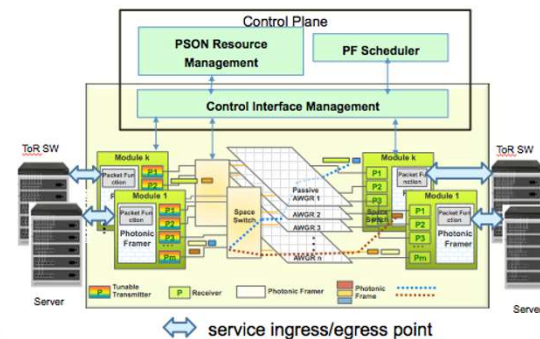
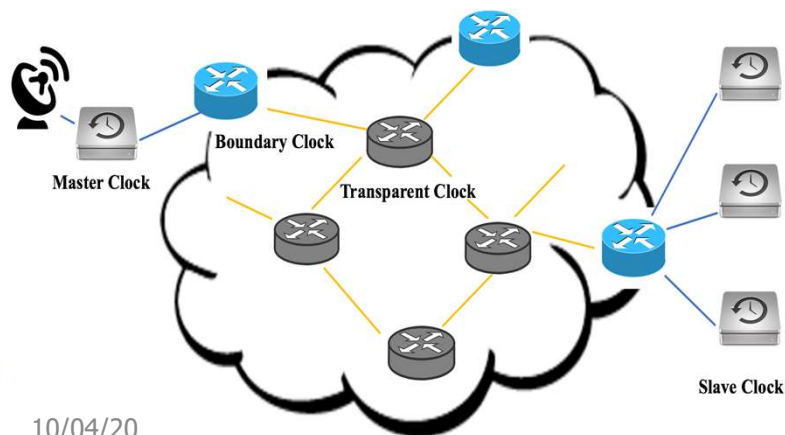
Time-error is the lowest for packet length of 200 bytes. Pareto distribution obtains highest time-error among others

Summary and Future Research Ideas

- Tested performance of PTP for a PSON datacenter architecture with zero-overhead and microsecond-accuracy.
- If the data packets are short and load is high PTP can achieve sub-microsecond accuracy

Future work:

- Implementing boundary clocks with multiple sub-networks
- Implementing an traffic adaptive resynchronization-time transmission



10/04/20

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Publications

- T. Ahmed, S. Rahman, M. Tornatore, K. Kim, B. Mukherjee, "A survey on high-precision time synchronization techniques for optical datacenter networks and a zero-overhead microsecond-accuracy solution," *Photonic Network Communications*, vol. 36, no. 1, pp. 56-67, Aug. 2018.

Outline

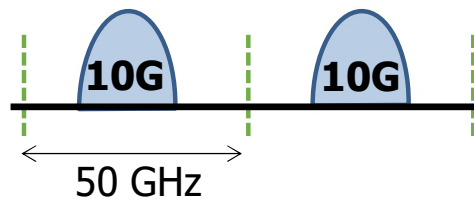
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Fixed-Grid Optical Link

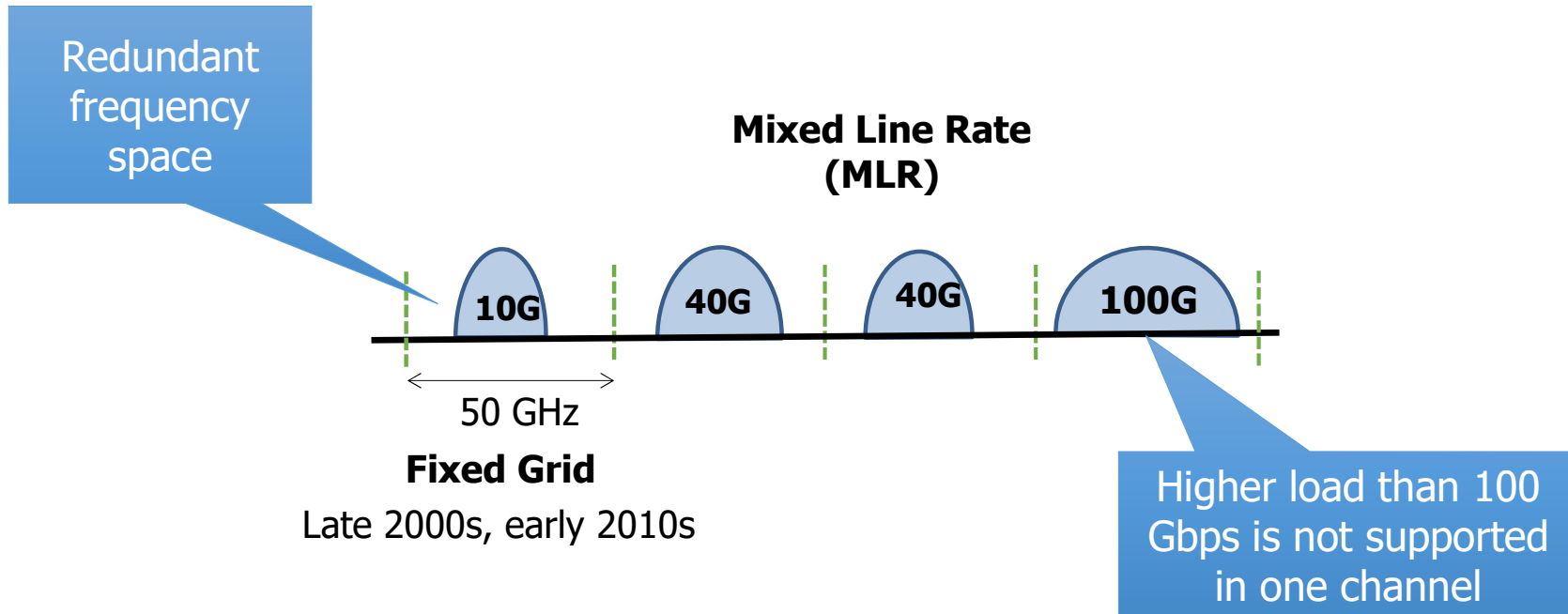
**Single Line Rate
(SLR)**



**Fixed
Grid**

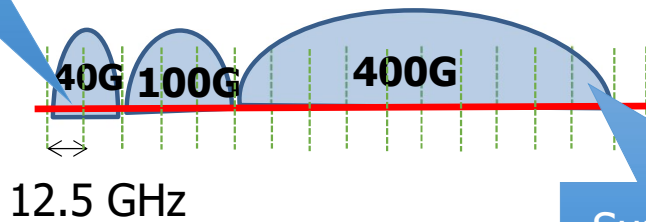
**Years 1990s,
2000s**

Fixed-Grid Optical Link



Flex-Grid Optical Link

Supports granular frequency



Flexible Grid

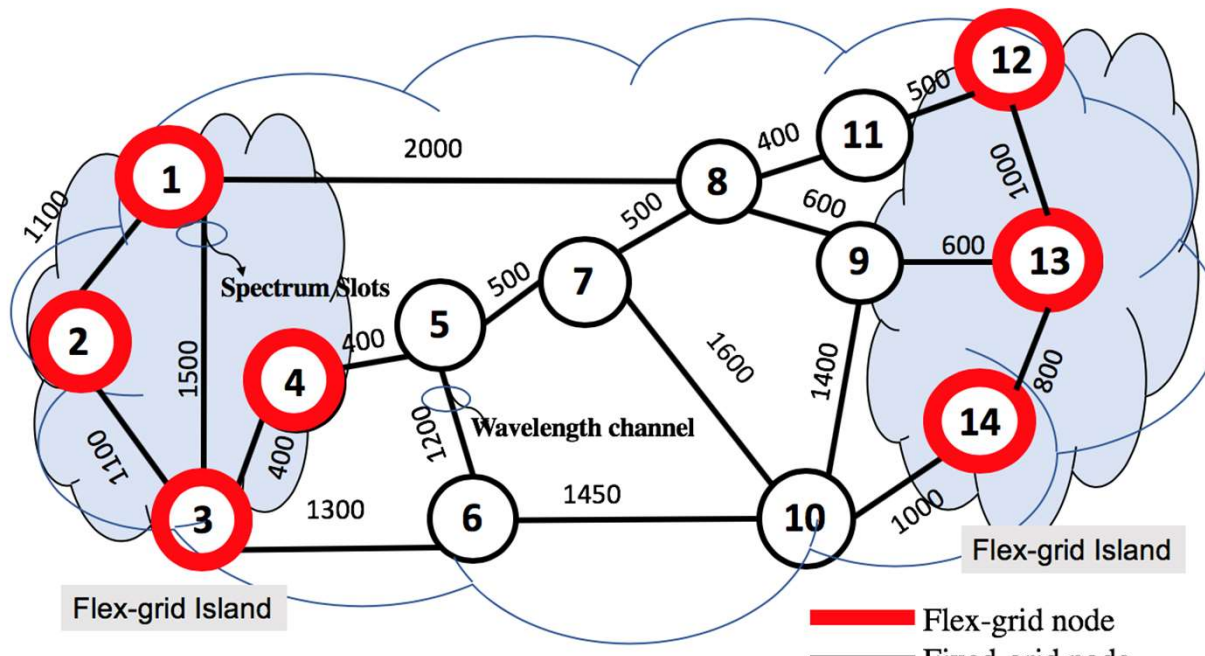
Supports higher load using super-channel

Improvement in spectrum usage

Bit-rate (Gbps)	Fixed (GHz)	Flex (GHz)
40	50	25
100	50	37.5
400	200	125

Starting 2011, ongoing research...

Migration from Fixed to Flex Grid: "Mixed-grid" Case



Migration decision depends on:

- Network load
- Population/DC placement
- Upgrade costs

Interoperability Challenge!

Spectrum and Modulation Format Assignment: Mixed-grid

Spectrum occupation for various bit-rates.

Traffic Demand (Gb/s)	Fixed-Grid		Flex-Grid	
	Bandwidth (GHz)	#Wavelengths	Bandwidth Gap (GHz)	# Slots
40	50	1	25	2
100	50	1	37.5	3
200	100	2	75	6
400	200	4	150	12

BPSK < QPSK < 8QAM < 16QAM < 32QAM

BPSK : Binary phase shift keying

QPSK : Quadrature phase shift keying

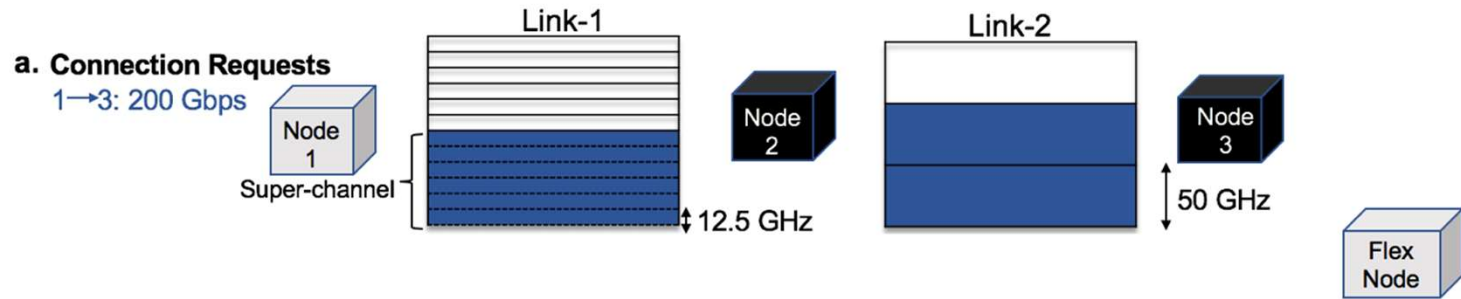
QAM: Quadrature amplitude modulation

Distance and spectrum occupation in flex-grid.

Traffic Demand (Gb/s)	Modulation Format	Operating Bandwidth (GHz)	Distance (km)	#Slots
40	BPSK	50	6000	4
	QPSK	25	3000	2
	8QAM	12.5	1000	1
100	BPSK	75	4500	6
	QPSK	50	3500	4
	QPSK	37.5	3000	3
	8QAM	25	2500	2
	16QAM	18.75	1500	2
200	BPSK	100	2500	8
	QPSK	75	1500	6
	8QAM	62.5	1000	5
	16QAM	43.75	700	4
	32QAM	37.5	500	3

Spectrum and Modulation Format Assignment: Mixed-grid

With QPSK



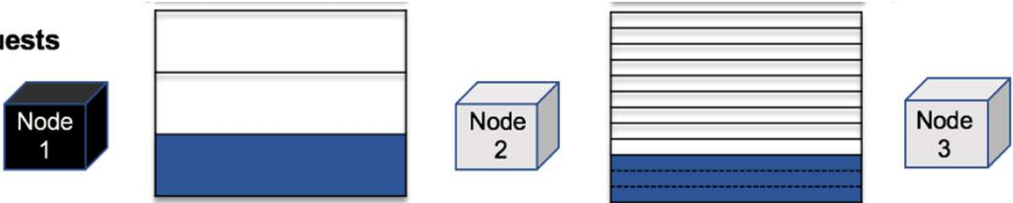
Spectrum occupation for various bit-rates.

Traffic Demand (Gb/s)	Fixed-Grid		Flex-Grid	
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400	200	4	150	12

Spectrum and Modulation Format Assignment: Mixed-grid

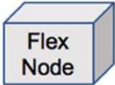
With QPSK

b. Connection Requests
1→3: 100 Gbps



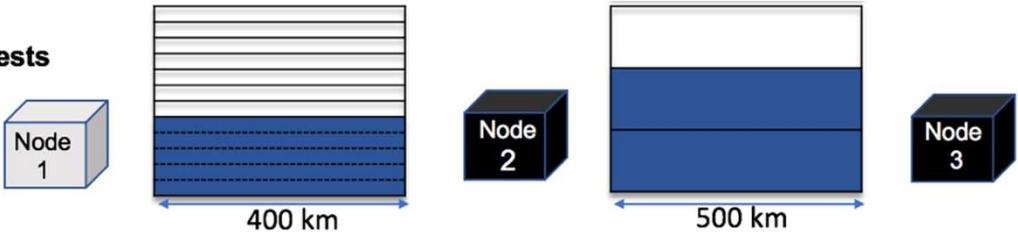
Spectrum occupation for various bit-rates.

Traffic Demand (Gb/s)	Fixed-Grid		Flex-Grid	
	Bandwidth (GHz)	#Wavelengths	Bandwidth Gap (GHz)	# Slots
40	50	1	25	2
100	50	1	37.5	3
200	100	2	75	6
400	200	4	150	12



Spectrum and Modulation Format Assignment: Mixed-grid

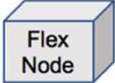
c. Connection Requests
 1→3: 200 Gbps
 (8QAM)



With Distance adaptive modulation format

Distance and spectrum occupation in flex-grid.

Traffic Demand (Gb/s)	Modulation Format	Operating Bandwidth (GHz)	Distance (km)	#Slots
40	BPSK	50	6000	4
	QPSK	25	3000	2
	8QAM	12.5	1000	1
100	BPSK	75	4500	6
	QPSK	50	3500	4
	QPSK	37.5	3000	3
	8QAM	25	2500	2
	16QAM	18.75	1500	2
200	BPSK	100	2500	8
	OPSK	75	1500	6
	8QAM	62.5	1000	5
	16QAM	43.75	700	4
	32QAM	37.5	500	3



Problem Statement

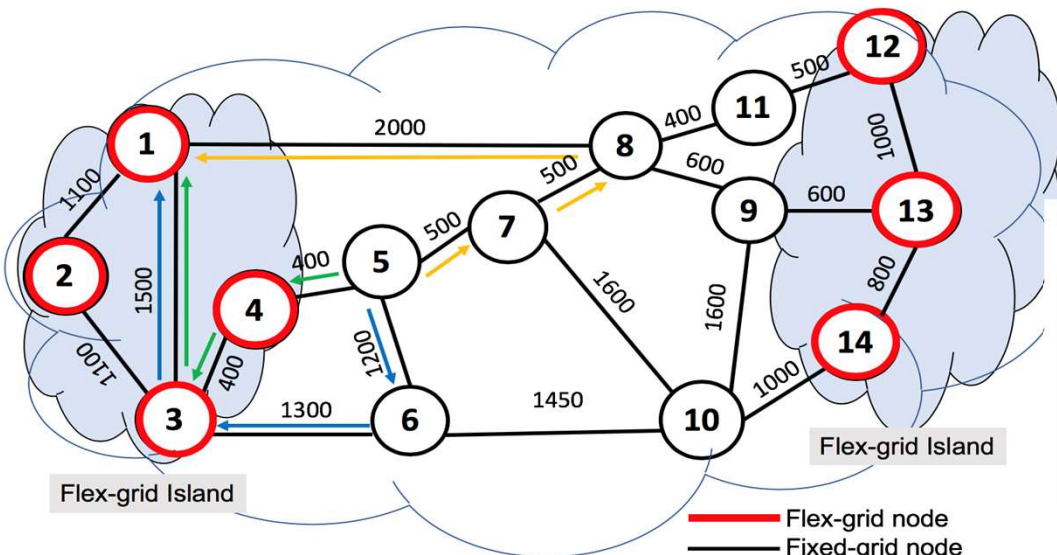
- Given:
 - Topology
 - Arrival rate of traffic flows
 - Set of traffic profiles
 - Set of fixed/flex-grid node locations with limited spectrum resources and constraints
- Objective:
 - *In a mixed-grid scenario provision optimal routes, spectrum, and modulation format with minimum bandwidth blocking*

Proposed Algorithm

Algorithm 1 Spectrum Efficient Dynamic Route and Spectrum Allocation (SEDRA)

```
1: Input:  $N(V, E), p_{s,d}, \alpha_{s,d}$ ;  
2: Output: Route, Spectrum, and Modulation Format;  
3: for each connection request ( $\alpha_{s,d}$ ) do  
4:    $P_{s,d} \leftarrow$  find set of k-shortest paths  $\alpha_{s,d}$ ;  
5:    $\triangleright$  list of candidate paths with available spectrum  
6:   for each  $p_{s,d}$  in  $P_{s,d}$  do  
7:     if ( $spectrum\_avail(p_{s,d}, \alpha_{s,d}) == True$ ) then  
8:        $\kappa_{s,d} \leftarrow \kappa_{s,d} \cup p_{s,d}$ ;  
9:     end if  
10:  end for  
11:  for each  $p_{s,d}$  in  $\kappa_{s,d}$  do  
12:     $m \leftarrow modulation\_format(p_{s,d}, \alpha_{s,d})$ ;  
13:     $\gamma_T^p \leftarrow calculate\_spectrum(p_{s,d}, \alpha_{s,d}, m)$ ;  
14:     $\triangleright$  find path requiring least spectrum for  $\alpha_{s,d}$   
15:    if  $\gamma_T^p$  is lowest then  
16:       $\gamma_{min}^p \leftarrow \gamma_T^p$ ;  
17:       $p_{s,d}^{best} \leftarrow p_{s,d}$ ;  
18:       $m^{best} \leftarrow m$ ;  
19:    end if  
20:  end for  
21:  Allocate lightpath on  $p_{s,d}^{best}$  using modulation format  
    $m^{best}$  to achieve minimum spectrum allocation of  $\gamma_{min}^p$ ;  
22: end for
```

Spectrum Efficient Dynamic Route and spectrum Allocation (SEDRA)

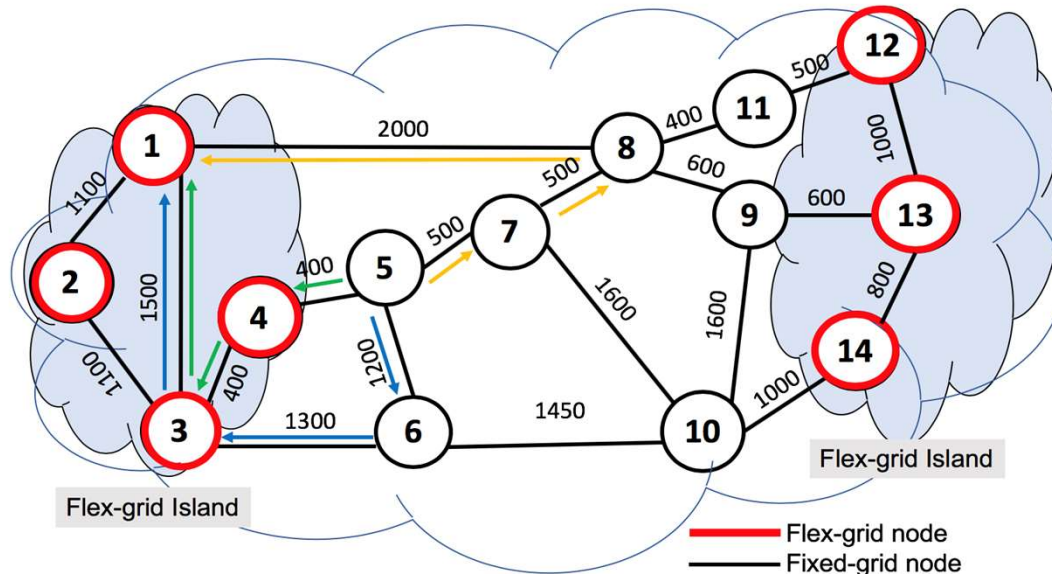


Spectrum occupation for various bit-rates.

Traffic Demand (Gb/s)	Fixed-Grid		Flex-Grid	
	Bandwidth (GHz)	#Wavelengths	Bandwidth Gap (GHz)	# Slots
40	50	1	25	2
100	50	1	37.5	3
200	100	2	75	6
400	200	4	150	12

- ✓ Path 1, 5-7-8-1 (3 fixed-grid & 1 flex-grid nodes): (50×3) GHz = 150 GHz
- ✓ Path 2, 5-4-3-1 (1 fixed-grid & 3 flex-grid nodes): $(50 + 37.5 \times 2)$ GHz = 125 GHz
- ✓ Path 3, 5-6-3-1 (2 fixed-grid & 2 flex-grid nodes): $(50 \times 2 + 37.5)$ GHz = 137.5 GHz

SEDRA with Distance-Adaptive Modulation Assignment (SEDRA-DA)



Distance and spectrum occupation in flex-grid.

Traffic Demand (Gb/s)	Modulation Format	Operating Bandwidth (GHz)	Distance (km)	#Slots
100	BPSK	75	4500	6
	QPSK	50	3500	4
	QPSK	37.5	3000	3
	8QAM	25	2500	2
	16QAM	18.75	1500	2

- ✓ Non-distance adaptive approach, 5-4-3-1 (1 fixed-grid & 3 flex-grid nodes, QPSK, 3000 kms):
 $(50 + 37.5 * 2)$ GHz = 125 GHz
- ✓ Distance adaptive (DA) approach, 5-4-3-1 (1 fixed-grid & 3 flex-grid nodes, 8QAM, 2500 kms):
 $(50 + 25 * 2)$ GHz = 100 GHz

Baseline Strategies

Routing:

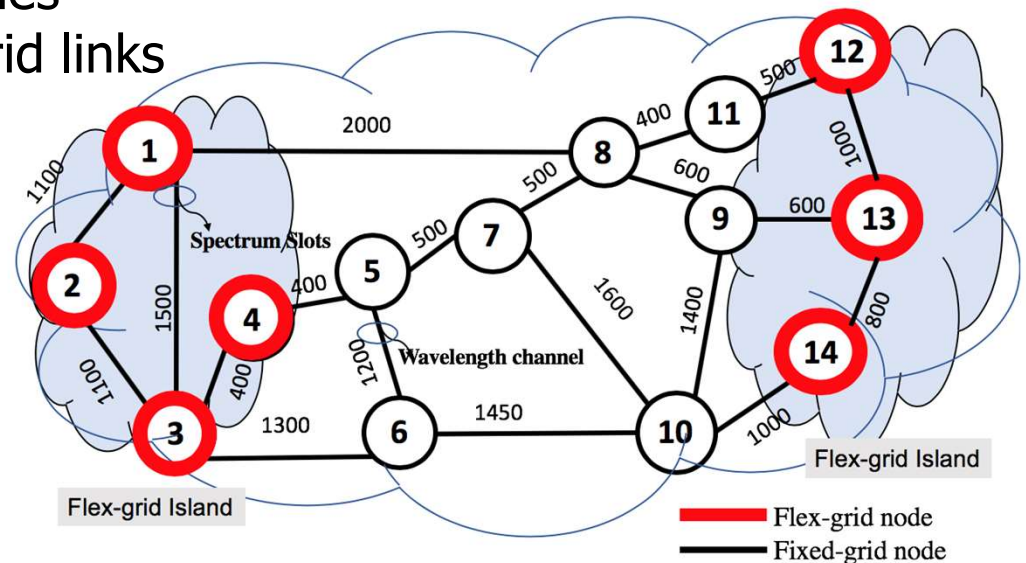
- Shortest Path First (SPF)
- Most Slots First (MSF)
- Largest Slot-over-Hops First (LSoHF)

Spectrum allocation:

- First Fit (FF)
- Random Fit (RF)
- Reusable Spectrum Allocation First (RSAF)

Simulation Setup

- 14 node NSFnet topology
- 7 flex-grid nodes and 7 fixed grid nodes
- 100 Wavelength channels for fixed-grid links
- 400 frequency slots for flex-grid links
- Poisson inter-arrival
- Exponential holding time

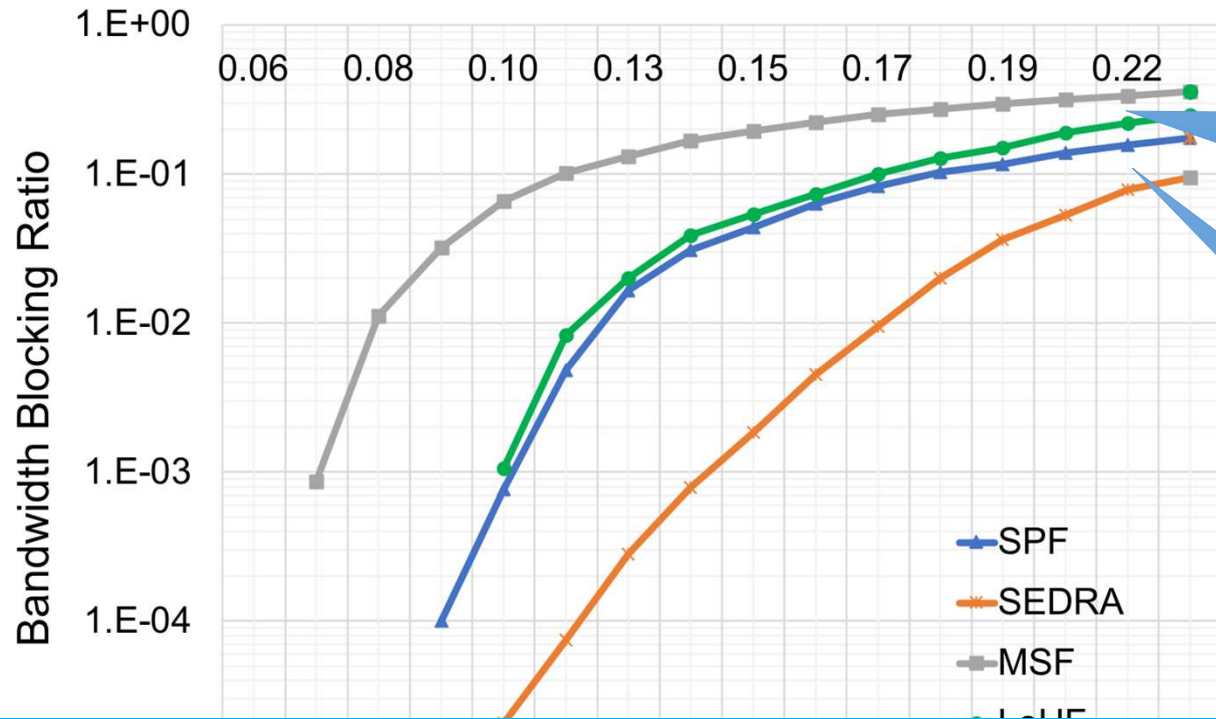


Performance Evaluation Metrics

$$\textit{Bandwidth blocking ratio} = \frac{\textit{Rejected bandwidth}}{\textit{Total requested bandwidth}}$$

$$\textit{Spectral utilization ratio} = \frac{\textit{Average spectrum occupied}}{\textit{Network Capacity}}$$

Results: BBR vs. Offered Load



BBR at 22% load
MSF 0.35
LoHF 0.24

BBR at 22% load
SPF 0.17
SEDRA 0.09

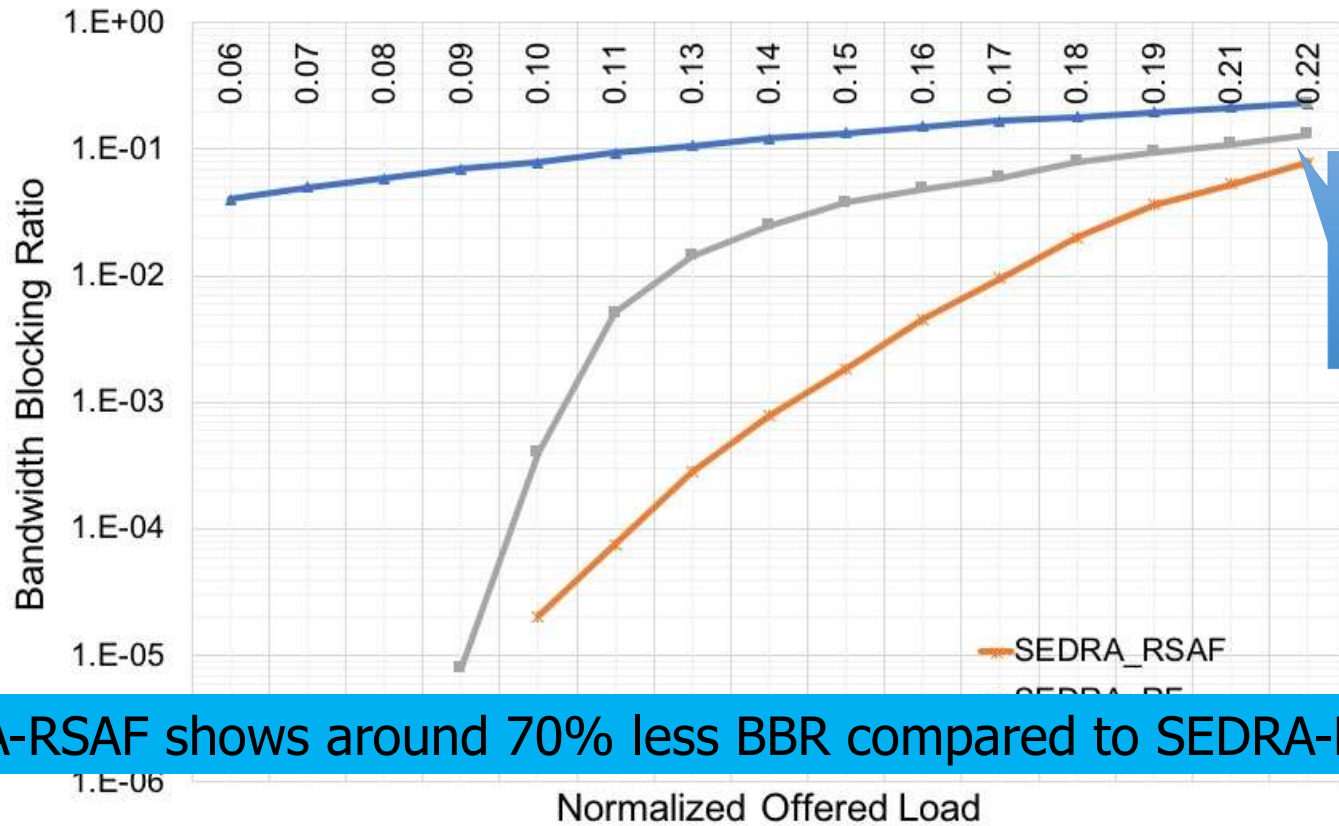
SEDRA shows around 80% less BBR compared to SPF

Normalized Offered Load

- Shortest Path First (SPF)
- Most Slots First (MSF)
- Largest Slot-over-Hops First (LSoHF)
- Spectrum Efficient Dynamic Route and spectrum Allocation (SEDRA)

Results: BBR vs. Offered Load

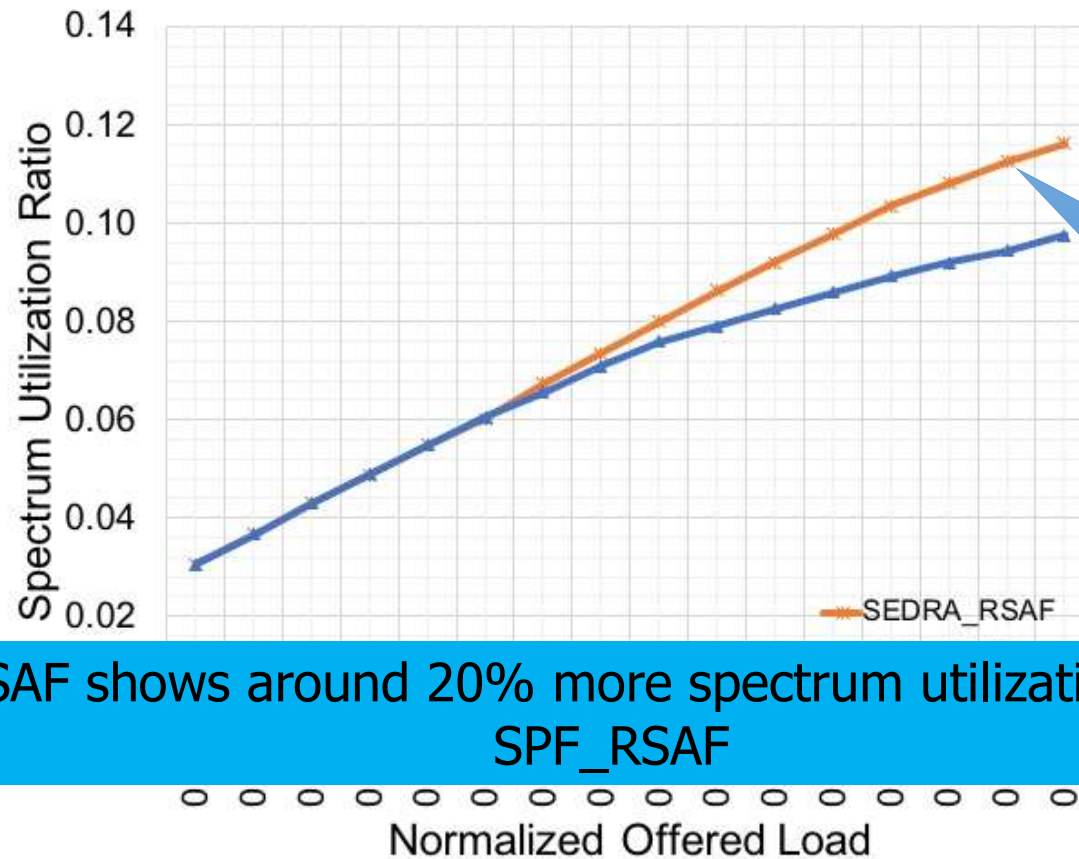
- First Fit (FF)
- Random Fit (RF)
- Reusable Spectrum Allocation First (RSAF)



SEDRA-RSAF shows around 70% less BBR compared to SEDRA-FF

Results: Spectrum Utilization vs. Offered Load

- Shortest Path First (SPF)
- Spectrum Efficient Dynamic Route and spectrum Allocation (SEDRA)
- Reusable Spectrum Allocation First (RSAF)

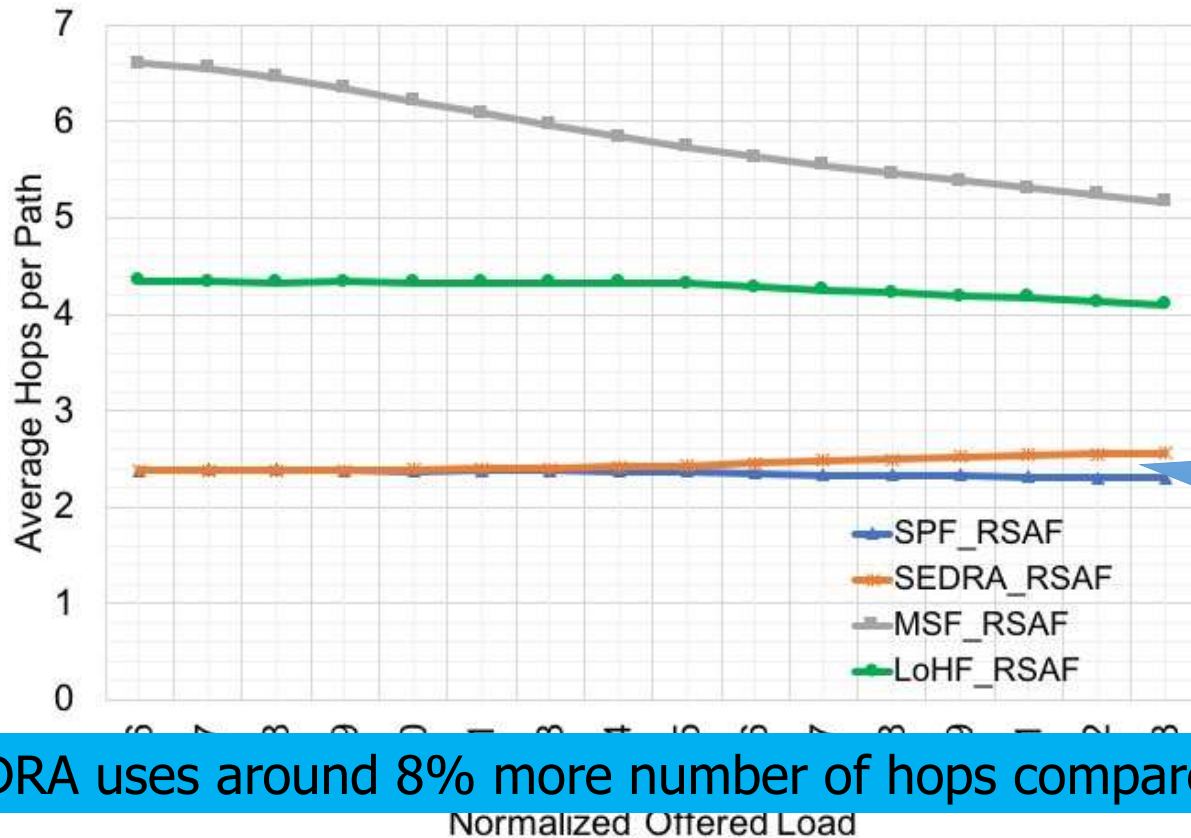


BBR at 22% load of SPF_RSAF 0.11
SEDRA_RSAF 0.09

SEDRA-RSAF shows around 20% more spectrum utilization compared to SPF_RSAF

Results: Average Hop Count vs. Offered Load

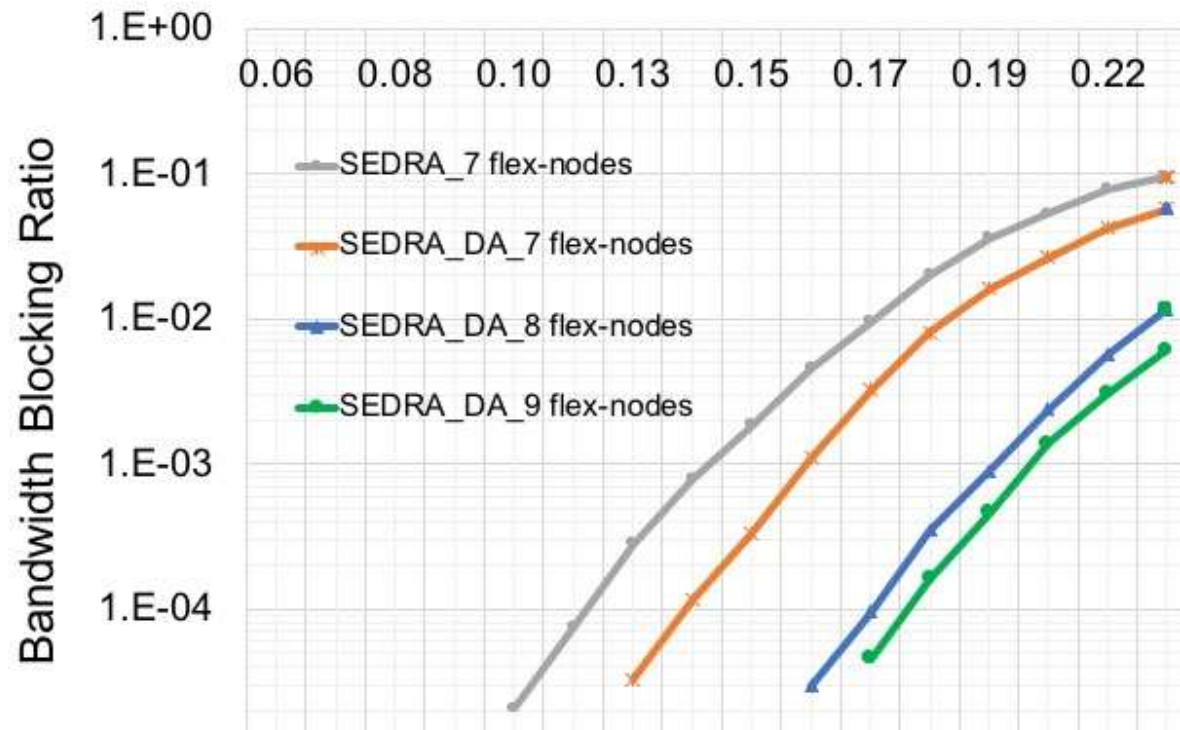
- Shortest Path First (SPF)
- Most Slots First (MSF)
- Largest Slot-over-Hops First (LSoHF)
- Spectrum Efficient Dynamic Route and spectrum Allocation (SEDRA)
- Reusable Spectrum Allocation First (RSAF)



Avg. hop count at 22% load
 SPF 2.3
 SEDRA 2.5

SEDRA uses around 8% more number of hops compared to SPF

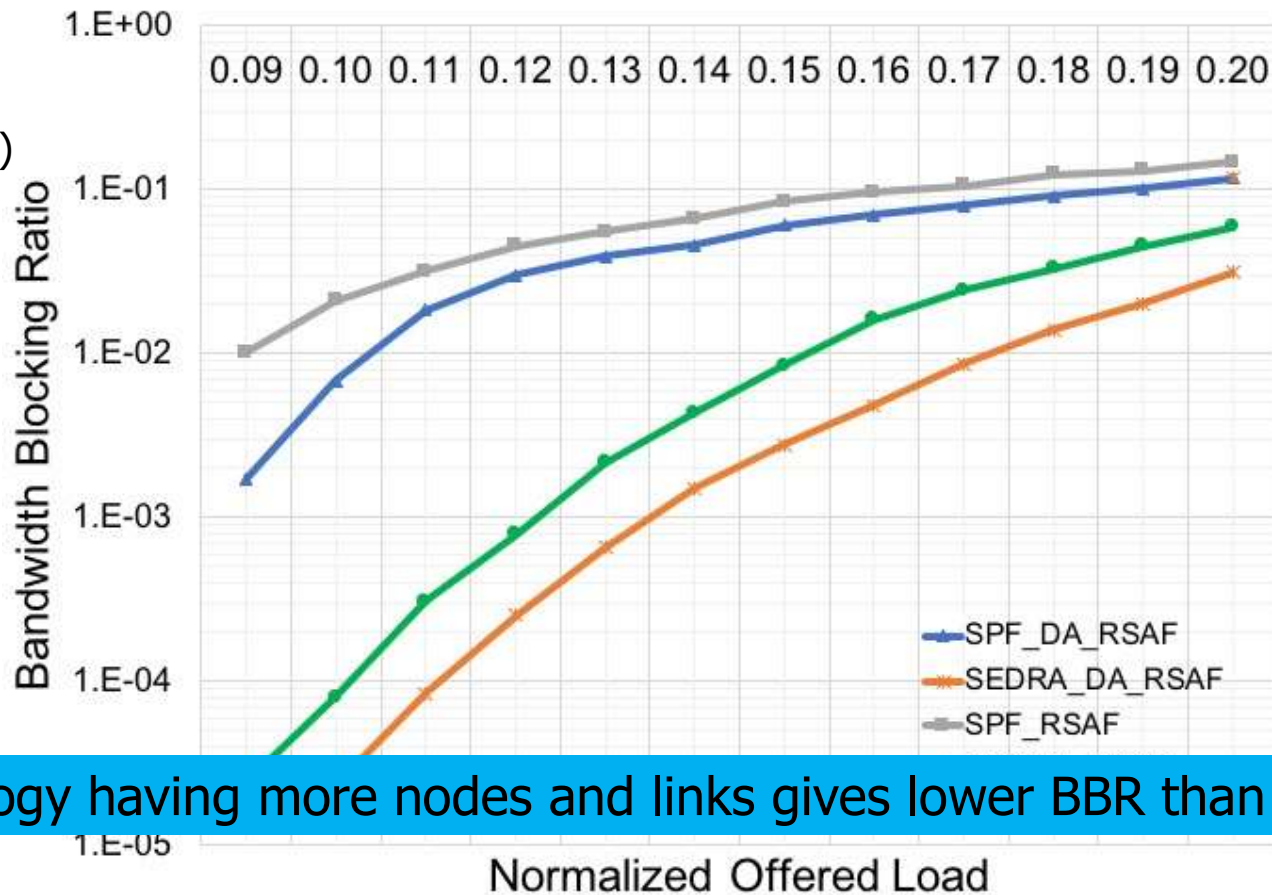
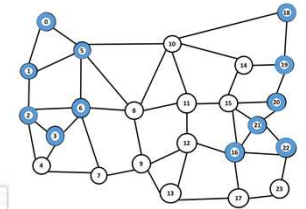
Results: BBR vs. Offered Load (varying no. of flex-grid nodes)



BBR decreases with increases number of flex-grid nodes

- Spectrum Efficient Dynamic Route and spectrum Allocation (SEDRA)
- Distance-adaptive modulation (DA)

Results: BBR vs. Offered Load (Usnet-24)



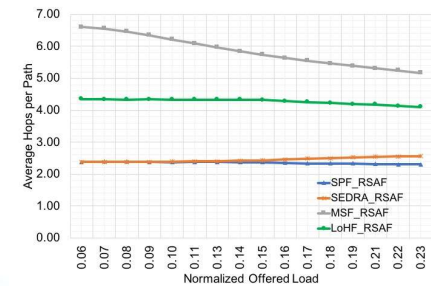
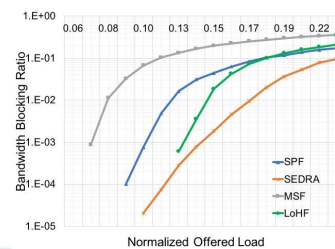
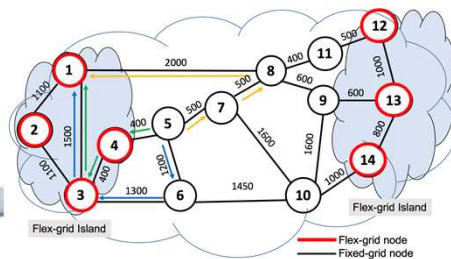
Usnet-24 topology having more nodes and links gives lower BBR than NSFnet-14

Summary and Future Research Ideas

- A mixed-grid-aware spectrum-efficient solution called SEDRA is proposed for a dynamic traffic scenario
- Illustrative results show **80%** BBR reduction with cost of **8%** increased hop count is achieved compared to SPF for NSFnet-14 network
- **20%** of spectrum utilization is obtained using SEDRA compared to SPF NSFnet network

Future work:

- Applying insights gained from analysis of SEDRA to take migration decisions



Publications

- T. Ahmed, S. Rahman, M. Tornatore, X. Yu, K. Kim and B. Mukherjee, "Dynamic Routing and Spectrum Assignment in Co-Existing Fixed/Flex-Grid Optical Networks," *Proc., Advanced Networks and Telecommunications Systems (ANTS)*, Indore, India, Dec. 2018.
- T. Ahmed, S. Rahman, S. Ferdousi, M. Tornatore, A. Mitra, B. C. Chatterjee, and B. Mukherjee, "Dynamic Routing, Spectrum, and Modulation Format Assignment in Co-Existing Mixed-Grid Optical Networks," to be submitted to *Journal of Optical Communications and Networking*.

Outline

- Introduction
- Contribution I: High-precision time synchronization techniques for optical datacenter networks and a zero-overhead microsecond-accuracy Solution
- Contribution II: Dynamic routing, spectrum, and modulation format assignment in co-existing fixed/flex-grid optical networks
- Conclusion and future research ideas

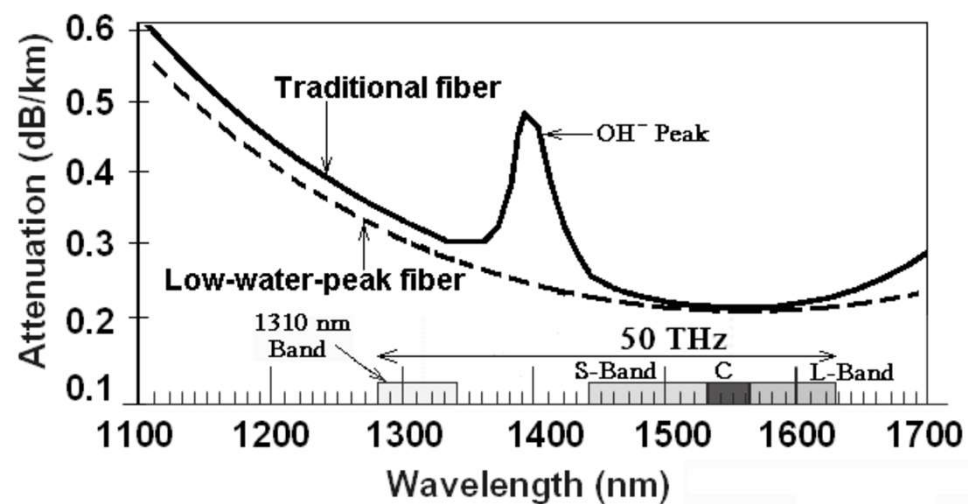
Outline

- ✓ Multiband optical line systems
- ✓ Spectrally–spatially flexible optical networks
- ✓ Spectrum trading in virtual optical networks

Multiband Optical Line Systems

C-band: 1530 nm to 1565 nm (Conventional) Lowest fiber loss

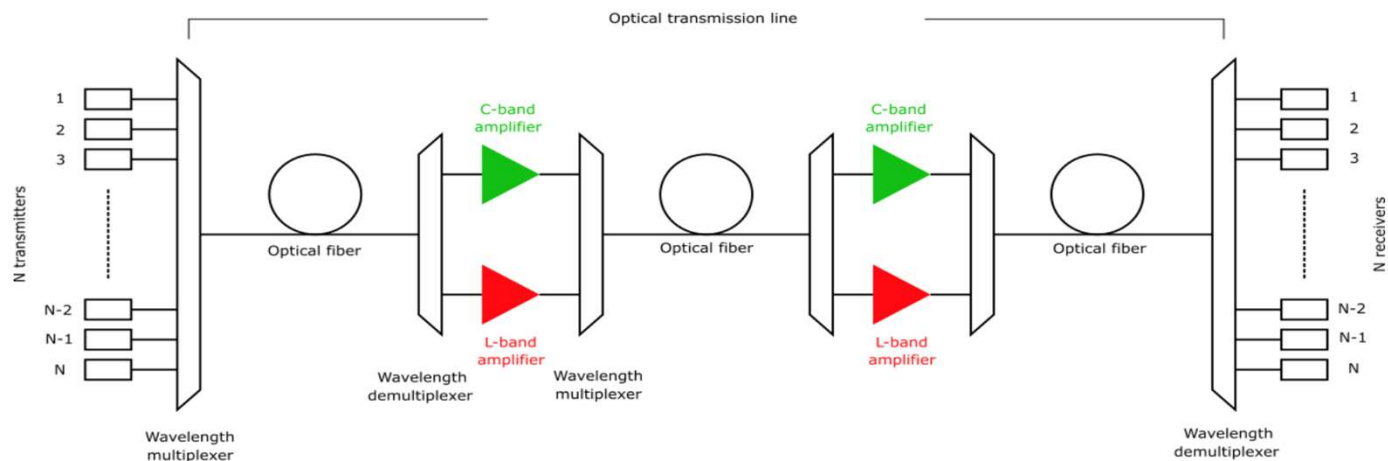
L-band: 1565 nm to 1625 nm (Long Band) Low attenuation



Source: B. Mukherjee, "Optical WDM Networks," *Springer Science & Business Media*, 2006.

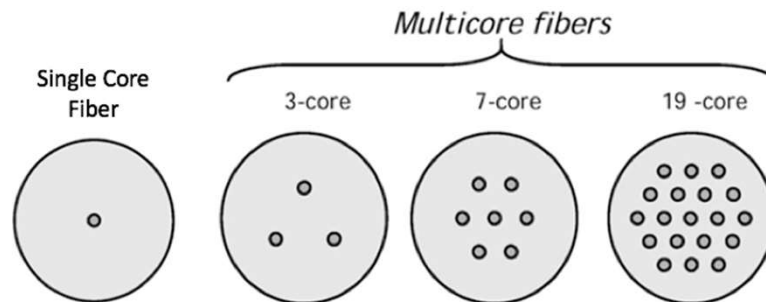
Challenges of Using Multiband Transmission

- Attenuation is higher than C band
- Quality-of-transmission estimator (QoT-E)
 1. Amplified spontaneous emission (ASE) noise
 2. Nonlinear impairments



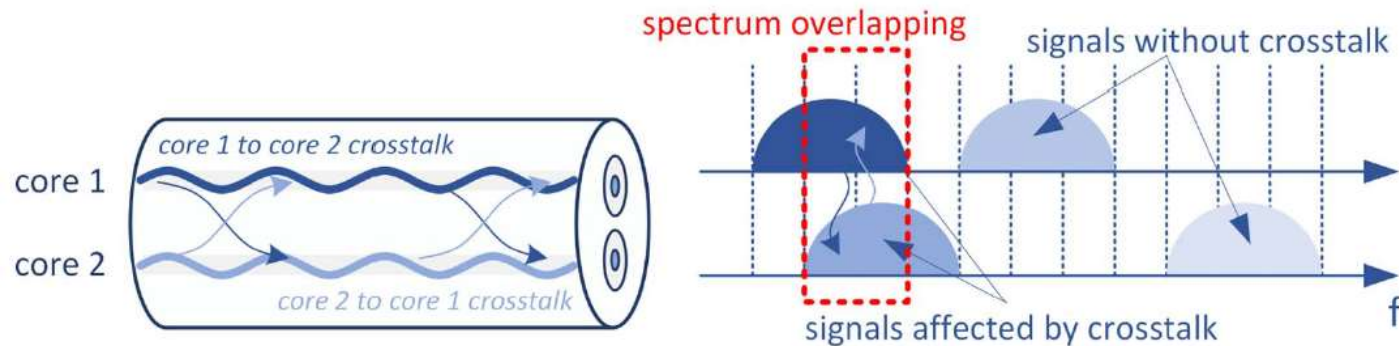
Spectrally–Spatially Flexible Optical Networks

1. Routing
2. Spectrum
3. Modulation format
4. Core



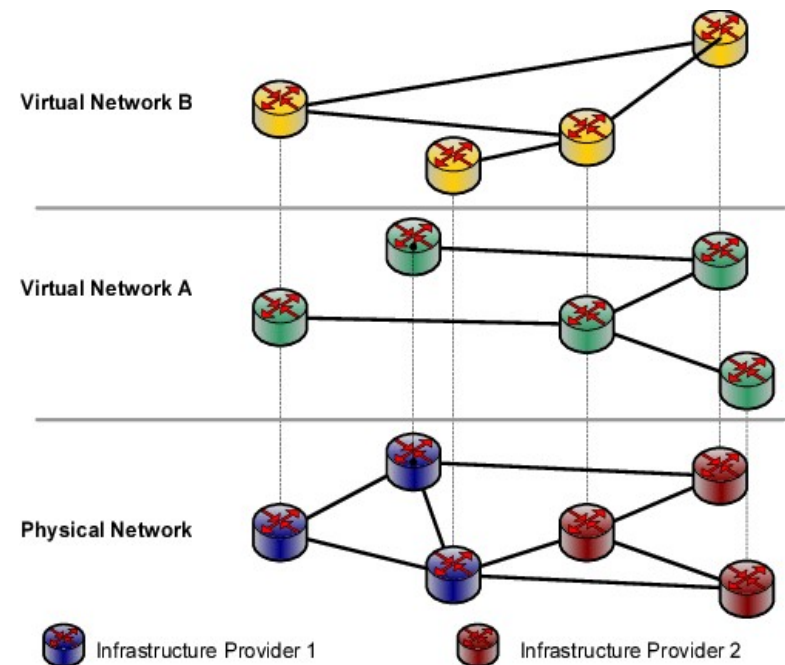
Courtesy: Andrea Marotta, Networks lab, UC Davis

Spectrally–Spatially Flexible Optical Networks

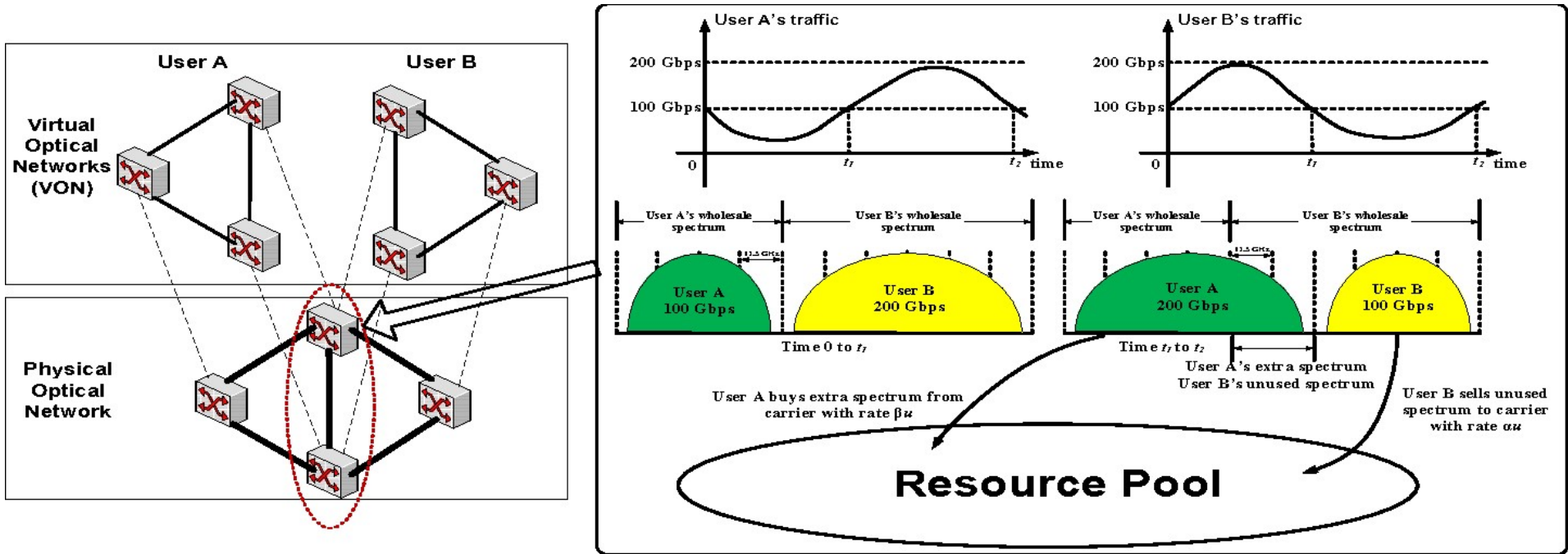


Spectrum Trading

- Network virtualization splits capacity of a physical network into multiple independent virtual optical networks (VONs)
- Allocated with fixed capacity
- Real-time capacity fluctuation
- Large idle capacity & capacity shortage is observed on virtual links



Spectrum Trading



Conclusion

- Importance of flexible network architecture
- Ultra low latency (sub-microsecond) is achievable in a distributed system like a datacenter using data plane transmission and PTP time synchronization protocol
- A mixed-grid-aware resource provisioning technique can obtain high spectrum efficiency by allocating lightpaths considering all the interoperability challenges



Appendix

Photonic Frame

OTS		ETSH		ETSP	
<u>OTa</u>	<u>OTfe</u>	<u>OTSt</u>	<u>OTSre</u>	PF Preamble	PF Payload

OTS: Optical Time Slot

ETS: Electrical Time Slot

ETSH: ETS Header

ETSP: ETS Payload

PF: Photonic Frame

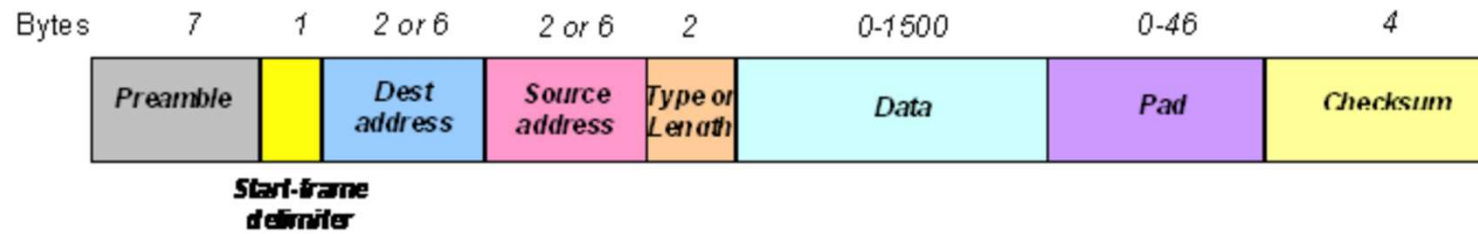
OTa: Optical guard time

OTfe: Optical Falling Edge time

OTSt: Optical wavelength Switching Time

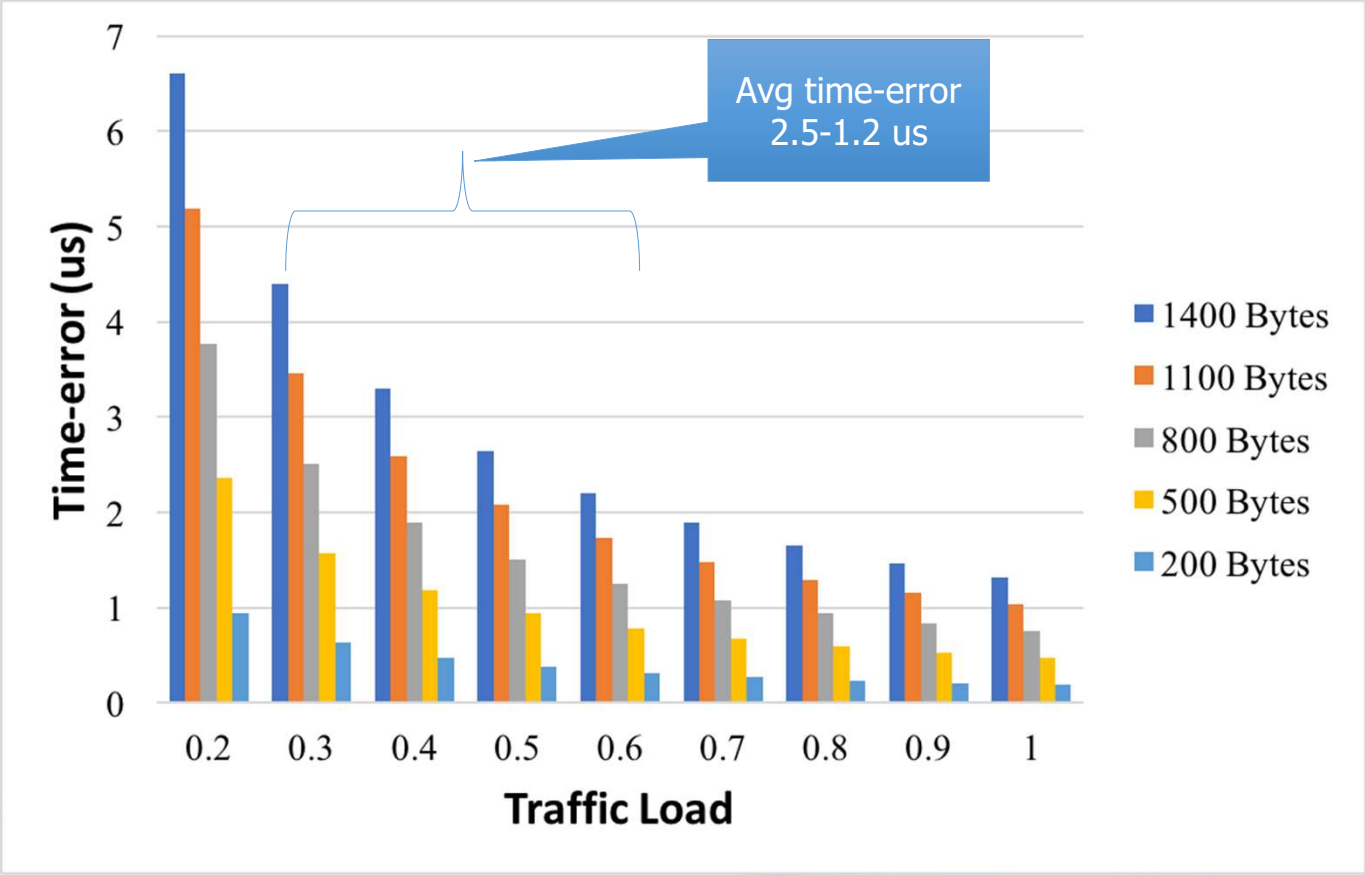
OTSre: Optical Rising Edge time

Ethernet Frame

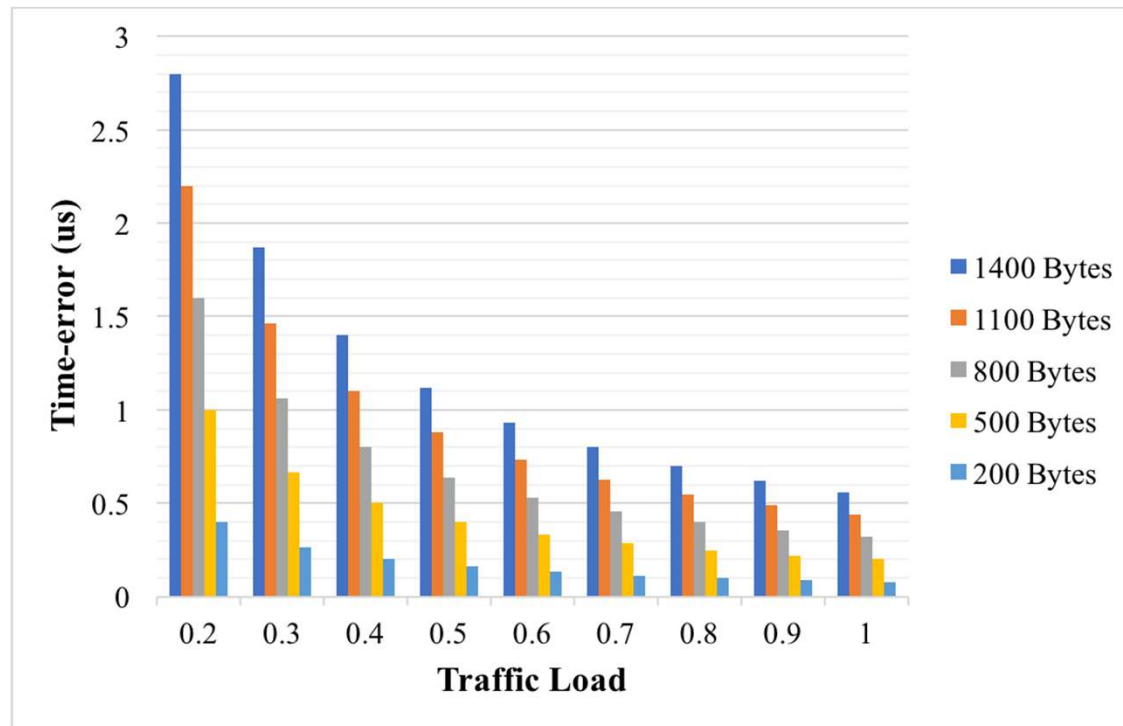


Source: <http://www.dcs.gla.ac.uk/~lewis/networkpages/m04s03EthernetFrame.htm>

Results: Time-error vs. Load (Pareto)



Results: Time-error vs. Load (Uniform)



Performance Evaluation Metrics

Offered load

= arrival rate * avg request size * avg holding time* Avg path length/Network Capacity

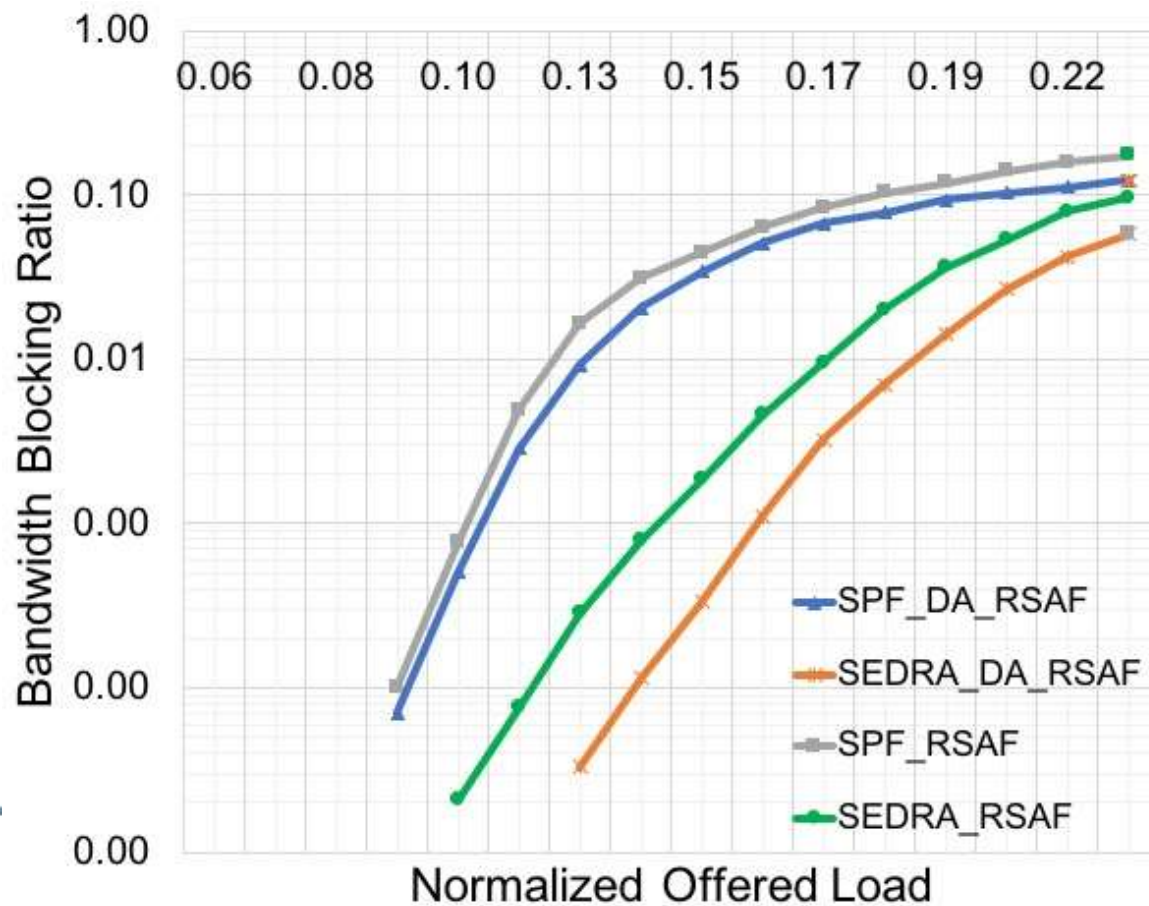
Network Capacity

= #fixed links * channel capacity in GHz * Spectral Efficiency of fixed grid +
#flex link * channel capacity in GHz * Spectral Efficiency of flex-grid

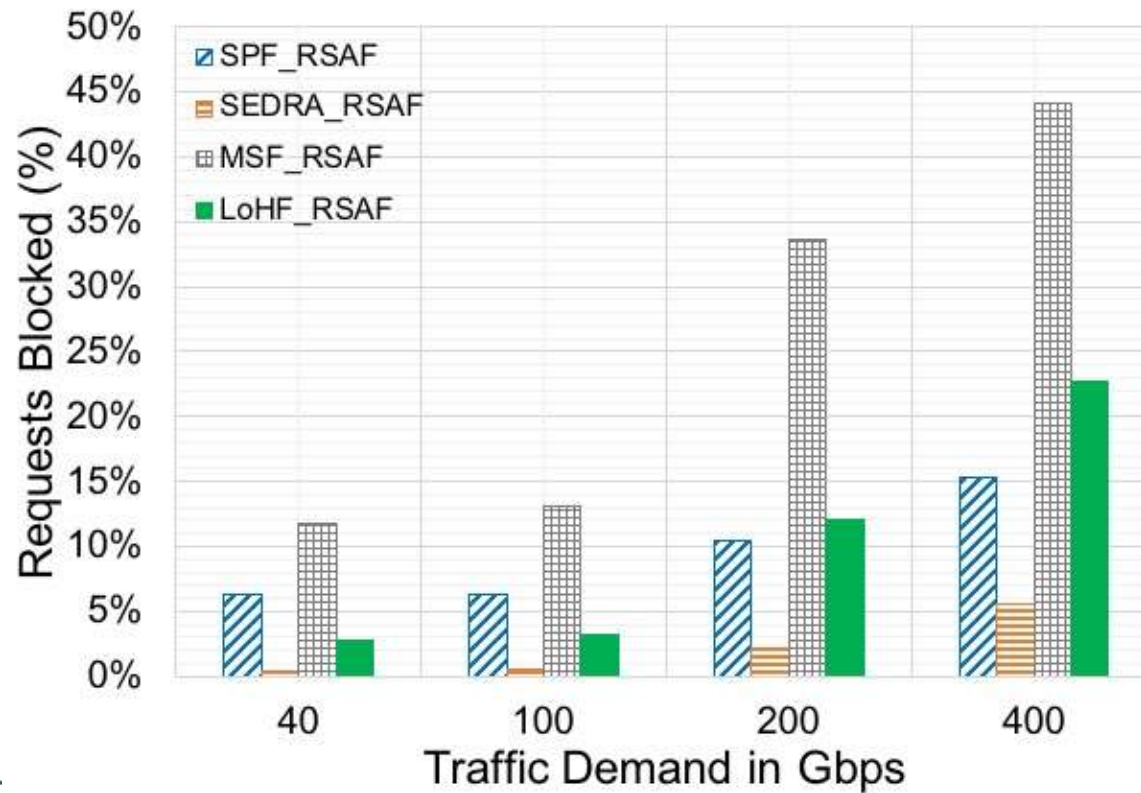
Spectral Efficiency of fixed grid = $100/50 = 2$ bits/sec/Hz

Spectral Efficiency of flex grid = $100/37.5 = 2.6$ bits/sec/Hz

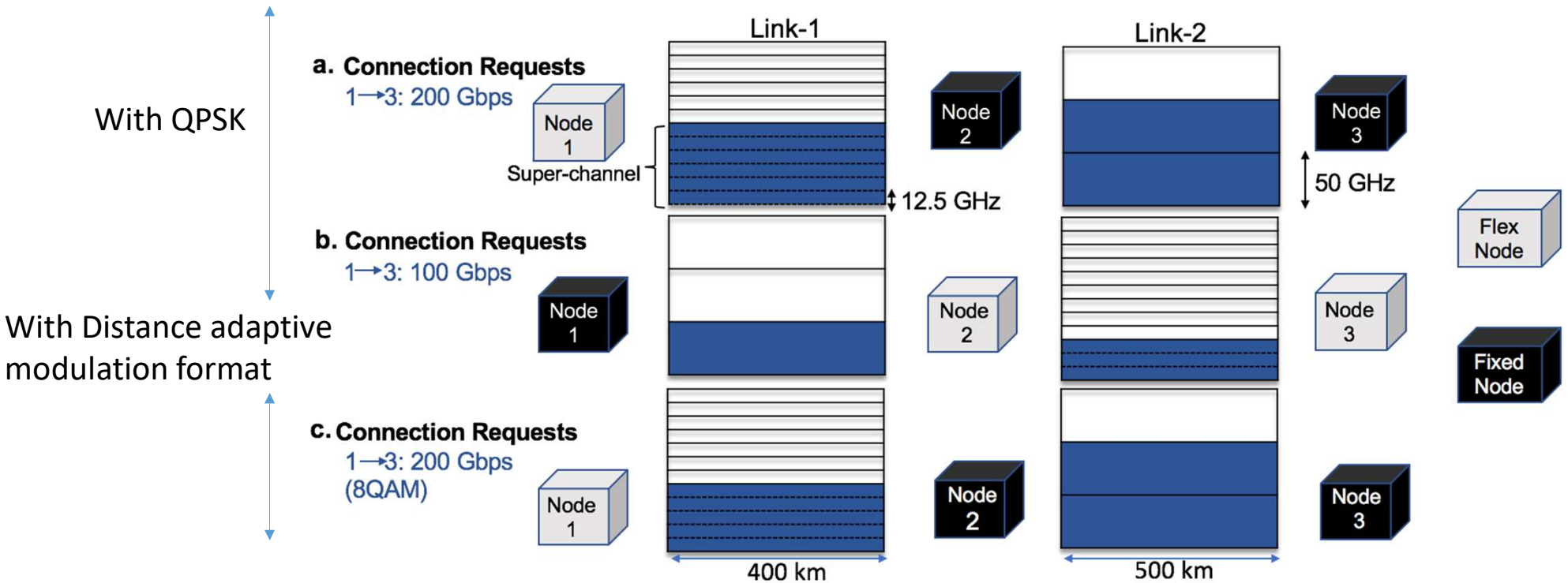
Results: BBR vs. Offered load



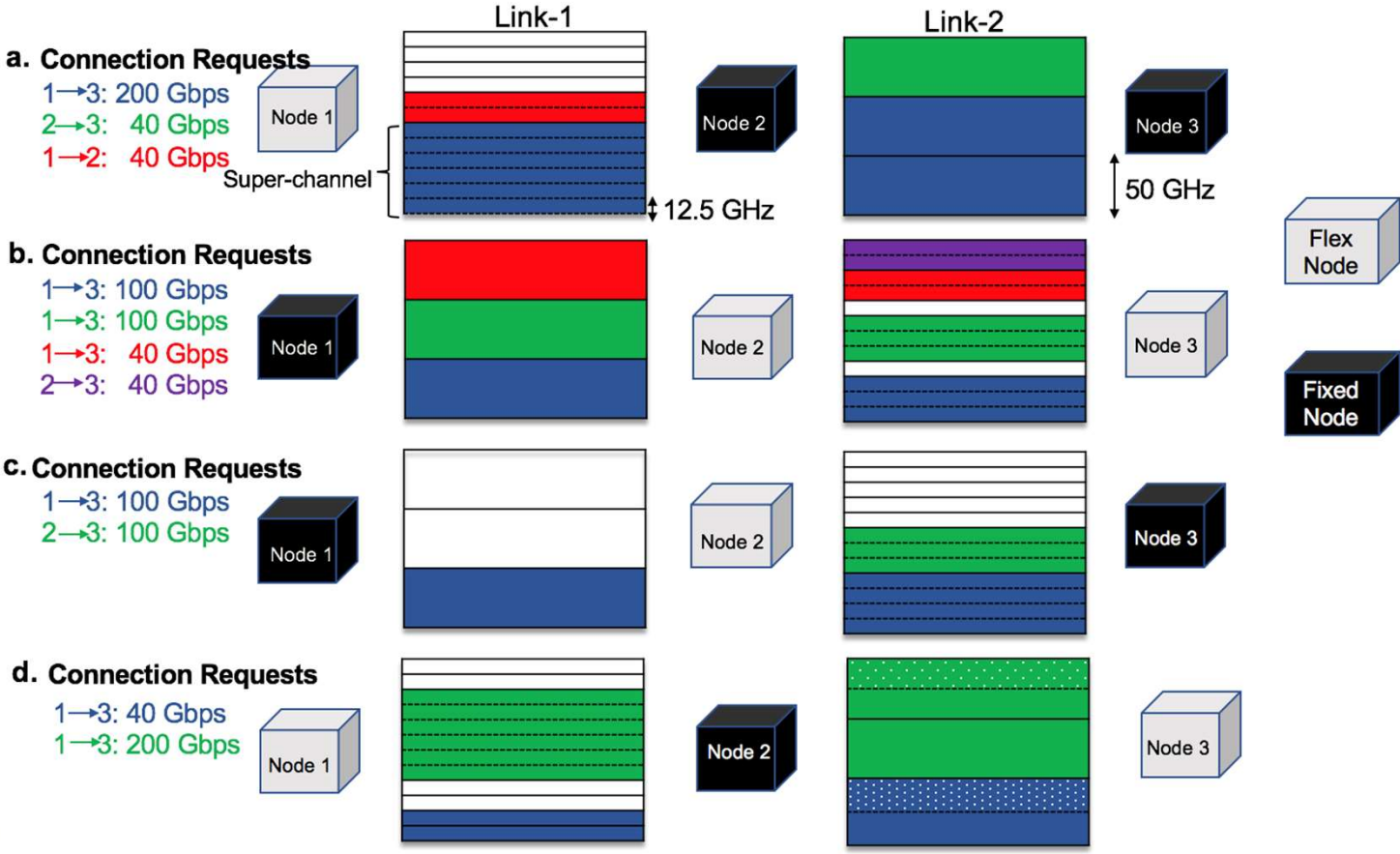
Results: Request Blocked vs. Traffic Demand



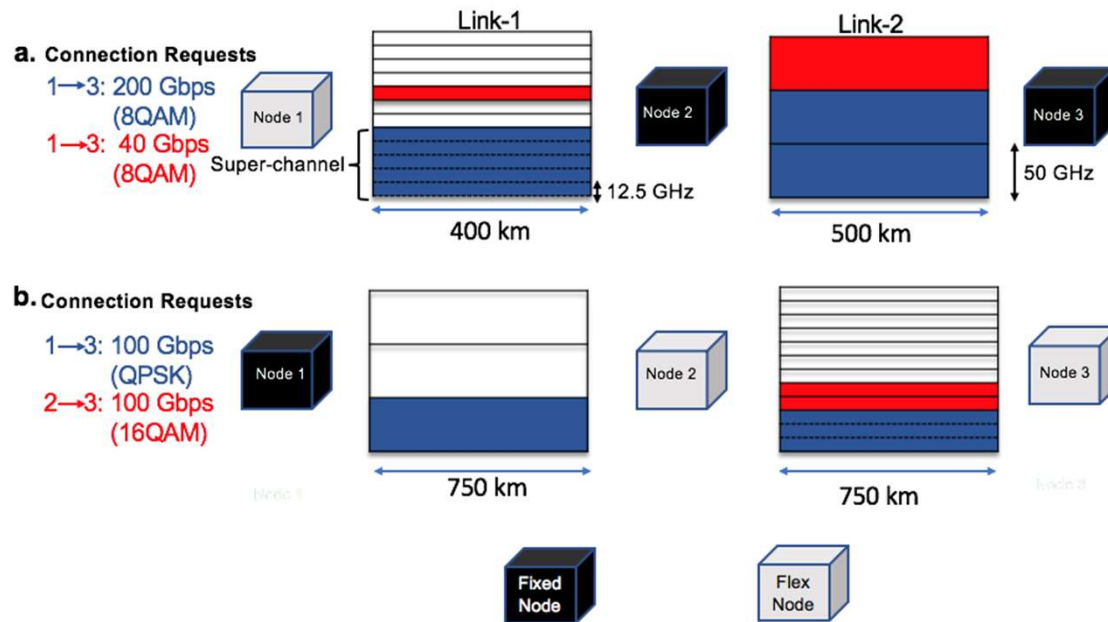
Spectrum and Modulation Format Assignment: Mixed-grid



Spectrum and Modulation Format Assignment: Mixed-grid



Spectrum and Modulation Format Assignment: Mixed-grid

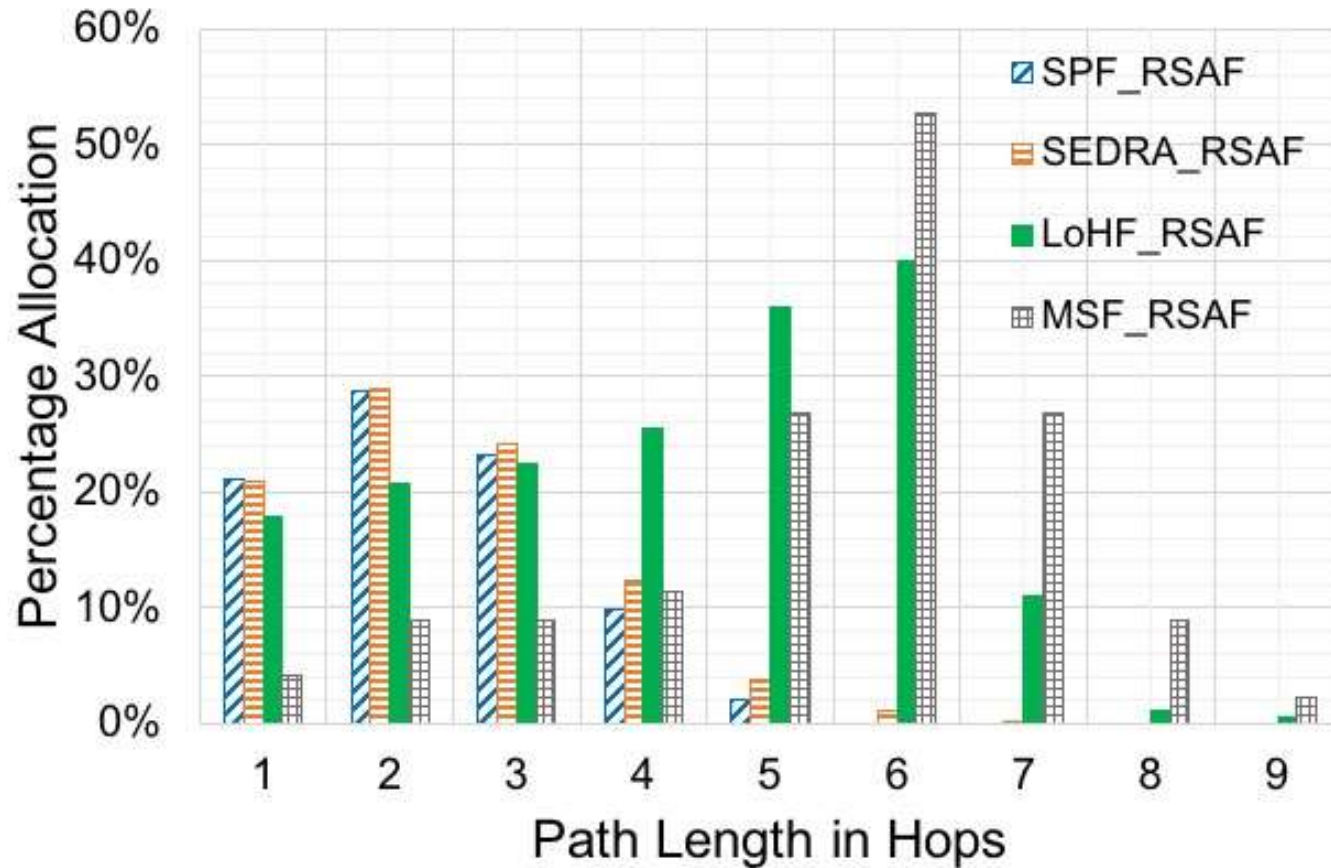


Traffic Profiles

Traffic Profiles

Traffic Demand (Gb/s)	Profile 1	Profile 2	Profile 3
40	50%	20%	0%
100	30%	50%	40%
200	15%	20%	40%
400	5%	10%	20%

Spectrum and Modulation Format Assignment: Mixed-grid



Proposed Algorithm

Algorithm 1 Spectrum Efficient Dynamic Route and Spectrum Allocation (SEDRA)

```

1: Input:  $N(V, E), p_{s,d}, \alpha_{s,d}$ ;
2: Output: Route, Spectrum, and Modulation Format;
3: for each connection request  $(\alpha_{s,d})$  do
4:    $P_{s,d} \leftarrow$  find set of k-shortest paths  $\alpha_{s,d}$ ;
5:    $\triangleright$  list of candidate paths with available spectrum
6:   for each  $p_{s,d}$  in  $P_{s,d}$  do
7:     if  $(\text{spectrum\_avail}(p_{s,d}, \alpha_{s,d}) == \text{True})$  then
8:        $\kappa_{s,d} \leftarrow \kappa_{s,d} \cup p_{s,d}$ ;
9:     end if
10:  end for
11:  for each  $p_{s,d}$  in  $\kappa_{s,d}$  do
12:     $m \leftarrow \text{modulation\_format}(p_{s,d}, \alpha_{s,d})$ ;
13:     $\gamma_T^p \leftarrow \text{calculate\_spectrum}(p_{s,d}, \alpha_{s,d}, m)$ ;
14:     $\triangleright$  find path requiring least spectrum for  $\alpha_{s,d}$ 
15:    if  $\gamma_T^p$  is lowest then
16:       $\gamma_{min}^p \leftarrow \gamma_T^p$ ;
17:       $p_{s,d}^{best} \leftarrow p_{s,d}$ ;
18:       $m^{best} \leftarrow m$ ;
19:    end if
20:  end for
21:  Allocate lightpath on  $p_{s,d}^{best}$  using modulation format
   $m^{best}$  to achieve minimum spectrum allocation of  $\gamma_{min}^p$ ;
22: end for

```

Proposed Algorithm

Algorithm 2 spectrum_avail()

```
1: Input:  $p_{s,d}, \alpha_{s,d}$ ;  
2: Output: Boolean, spectrum available or not;  
3:  $m \leftarrow \text{modulation\_format}(p_{s,d}, \alpha_{s,d})$ ;  
4: for each link  $l$  in  $p_{s,d}$  do  
5:    $\gamma_l^p \leftarrow \text{mixed\_grid\_spectrum}(s, l_s, l_e, \alpha_{s,d}, m)$ ;  
6:   Requested no. of slots,  $n \leftarrow \gamma_l^p / W_{fl}$ ;  
7:    $\triangleright$  find  $n$  contiguous slots on link  $l$   
8:   if  $\psi_l^n == \text{false}$  then  
9:     return false;  
10:  end if  
11: end for  
12: return true;
```

Proposed Algorithm

Algorithm 3 `mixed_grid_spectrum()`

```
1: Input:  $s, l_s, l_e, \alpha_{s,d}, m$ ;  
2: Output:  $\gamma_i^p$ ;  
3: if  $\phi_s == 0$  then  
4:   if  $\phi_{l_s} == 0$  then  
5:     calculate_spectrum(0,  $\alpha_{s,d}, m$ )  
6:      $\triangleright$  check node type: fixed/flex-grid;  
7:   else if ( $\phi_{l_s} == 1$  &  $\phi_{l_e} == 0$ ) then  
8:     calculate_spectrum(0,  $\alpha_{s,d}, m$ );  
9:   else if ( $\phi_{l_s} == 1$  &  $\phi_{l_e} == 1$ ) then  
10:    calculate_spectrum(1,  $\alpha_{s,d}, m$ );  
11:   end if  
12: else  
13:   if  $\phi_{l_s} == 1$  then  
14:     calculate_spectrum(1,  $\alpha_{s,d}, m$ );  
15:   else if ( $\phi_{l_s} == 0$  &  $\phi_{l_e} == 1$ ) then  
16:     calculate_spectrum(0,  $\alpha_{s,d}, m$ );  
17:   else if ( $\phi_{l_s} == 0$  &  $\phi_{l_e} == 0$ ) then  
18:     calculate_spectrum(0,  $\alpha_{s,d}, m$ );  
19:   end if  
20: end if  
21: return  $\gamma_i^p$ ;
```

Proposed Algorithm

Algorithm 4 calculate_spectrum()

```
1: Input:  $\phi_v, \alpha_{s,d}, m$ ;  
2: Output:  $\gamma_T^p$ ;  
3:  $\gamma_T^p \leftarrow 0$ ;  
4: for each link  $l$  in  $p_{s,d}$  do  
5:    $\gamma_l^p \leftarrow$  find minimum required spectrum for  $\alpha_{s,d}$  and  
   modulation format  $m$  from Table I and II;  
6:    $\gamma_T^p \leftarrow \gamma_T^p + \gamma_l^p$ ;  
7: end for  
8: return  $\gamma_T^p$ ;
```

Algorithm 5 modulation_format()

```
1: Input:  $p_{s,d}, \alpha_{s,d}$ ;  
2: Output:  $m$ ;  
3:  $p^l \leftarrow$  find path-length of path  $p_{s,d}$ ;  
4:  $p^{fixed} \leftarrow$  find if  $p_{s,d}$  has all fixed-grid nodes;  
5: if  $p^{fixed} == True$  then  
6:   return QPSK;  
7: else  
8:   return highest modulation format with reach  $p^l$  for  $\alpha_{s,d}$   
   using II;  
9: end if
```
