MAN Optimization via Clog Computing for a Heterogeneous Internet of Things

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Group Meeting

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Outline

- Purpose/Motivation
- Problem Statement
- Application Profiles
- Network Parameters/Costs
- Mathematical Description
- Topology/Flow Scenarios
- Simulation Results
- Ongoing Work



Purpose/Motivation

- Will IoT simply require more physical layer core capacity? Or will traffic nature, i.e. increased heterogeneity and functional requirements require more robust traffic engineering and/or policy based/constraint-based routing?
- Application Heterogeneity:
 - Bandwidth/Latency
 - Processing
 - Storage
 - Internal vs External to MAN
- MAN should play a more active role linking the access and core layers
 - fog processing and storage capabilities/cloud providers extend services to fog
- With increased application/traffic heterogeneity in IoT, effective traffic engineering & functional placement will have a much more significant impact on network costs and performance.

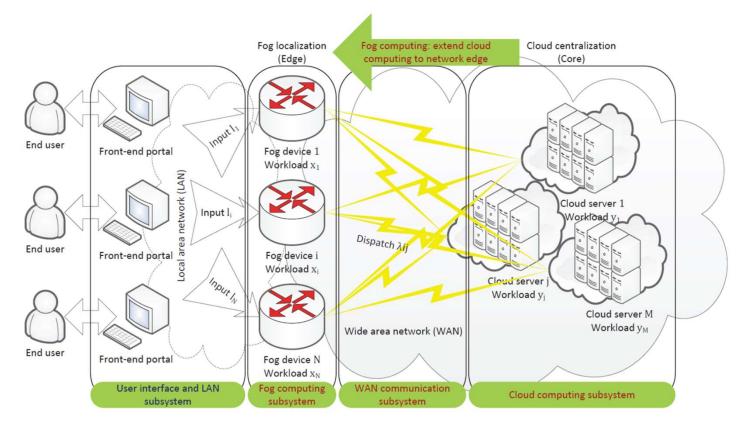


Problem Statement

- As IoT related traffic becomes increasingly heterogeneous and demands greater proportions of overall Internet traffic, it must be provisioned according to its unique performance and functional requirements, in this case: latency, throughput, processing, and storage requirements. MAN providers are in a unique position to manage and execute this function within a Hybrid Fog-Cloud environment. Thus a MAN provisioning model is proposed.
- Given core network SLAs, MAN topology/nodal capabilities, and performance requirements by app profile: minimize operational costs of MAN via 3 components:
 - Path from source to destination intra-MAN
 - Path from source to MAN/WAN interface external traffic
 - Processing/Storage Nodes (if applicable):
 - Fog/Cloud/Hybrid
- Goal is to model mixtures of anticipated application/traffic profiles routed through a MAN with maximum end-to-end latency via constraint-based routing principles to demonstrate what factors (application/topological parameters) have a more significant impact on total costs.



Related Work

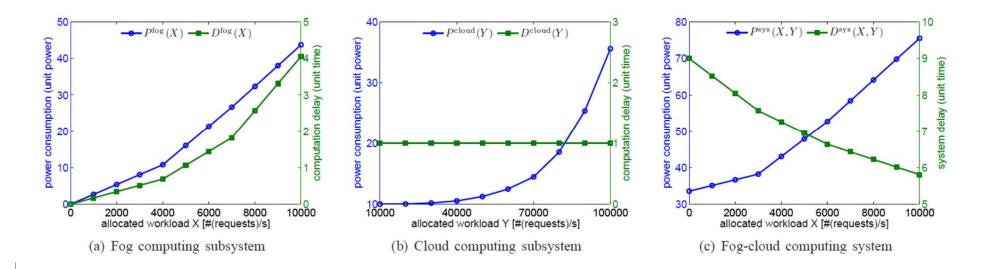


System with four subsystems, focuses on workload and relationships between each subsystem: LAN/input, Fog, WAN, Cloud



Deng, Ruilong, et al. "Optimal Workload Allocation in Fog-Cloud Computing Towards Balanced Delay and Power Consumption." (2012).

Related Work



Fog subsystem:

Computation delay increases with power consumption

Cloud subsystem:

Computation delay remains relatively fixed for increased power consumption

Fog-Cloud Computing system:

Total system delay decreases with increasing power consumption

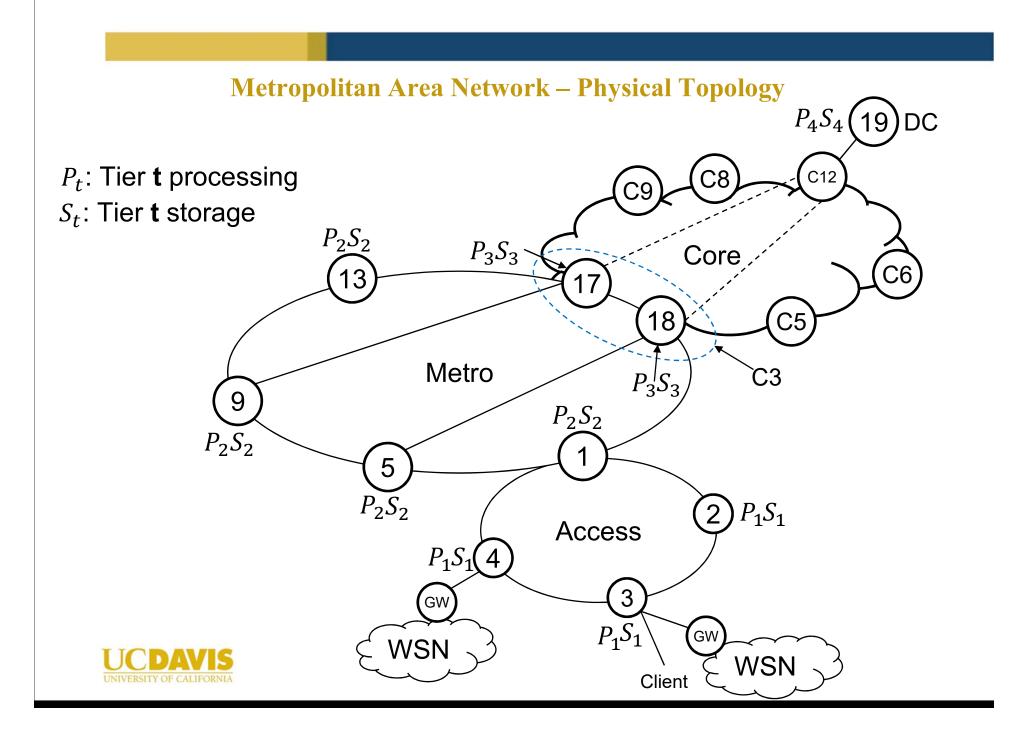


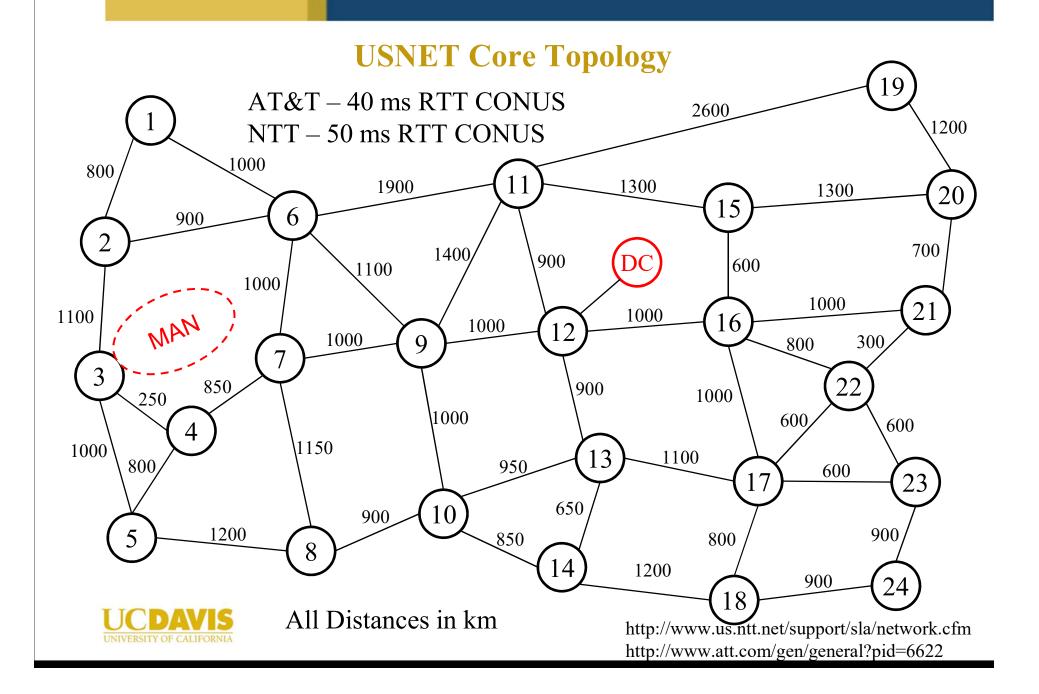
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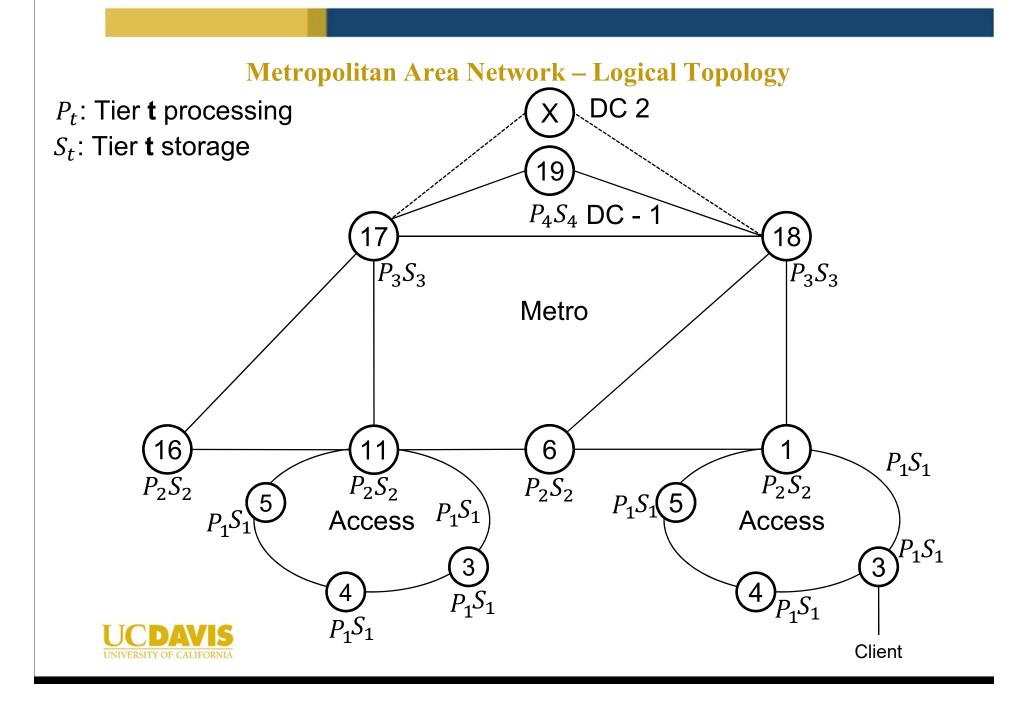
Mathematical Explanation

- Inputs:
 - MAN Topology: G(N,L) (and core location)
 - Node tier dictates costs and capacities for processing and storage $-\mu$, ν , U, E
 - DC location in core
 - Costs per unit traffic: Λ MAN, ϵ WAN
 - Application Profiles:
 - α, β, κ, Δ, Θ
 - Core Network SLAs: Residual Latency by application & destination $\theta_{a,f}$
- Objective function: Minimize total operational cost of MAN
 - Processing, Storage, WAN up/down, Capacity
- Outputs: For all node pairs, profiles, and core destinations:
 - Path
 - Processing node (if applicable)
 - Storage node (if applicable)
 - Required link capacities, WAN bandwidth up/down









Application Profile

- Each application profile contains a unique combination of parameters:
- α: Computational complexity per unit of traffic
- β: Ratio of processed to raw data at processing node
- κ: Average flow size must be processed as a single entity
- A: Minimum storage time
- Θ : Uni-directional latency budget from access/GW to access/GW

App Profile	a (CPU/Mbps)	β	к (Mb)	Λ (hrs)	Θ (ms)
1- VR	0.01	0.2	3	0	50
2 - Indust Data	0.009	0.1	2	10	70
3 – Data Backup	0	0	0.5	4	210
4 - P-P interactive	0.007	0.3	0.4	0	50
5 - Encrypted Data	0.008	1.2	0.2	5	120
6 – P-P streaming	0	0	.001	0	130
7 – Medical	0.003	0.2	2	0.1	80
8 – Env Data	0.006	0.3	1	100	130
9 -	0	0	5	3	180



http://www.cisco.com/c/en/us/solutions/collateral/enterprise-networks/ enterprise-network-functions-virtualization-nfv/datasheet-c78-736768.html

Network Parameters

- Each application profile contains a unique combination of parameters
- µ: Per unit cost of computational power
- v: Per unit cost of storage capacity
- A: Per unit cost of MAN link capacity
- ε_{up} , ε_{down} : Per unit WAN bandwidth cost (up/down)
- τ: Processing time constant (Normalized to DC)

Tier	μ (\$/CPU/Mo)	v (\$/GB/Mo)	Л (\$/Mbps/Mo)	ε _{up} , ε _{down} (\$/Mbps)	τ (/CPU)
1 – Access CO	40	0.0042	0.005	.05/.01	3
2 – Metro CO	35	0.004	0.005	05/.01	2
3 – Core CO	30	0.0035	0.005	05/.01	1.5
4 - DC	25	0.0025	0.005	05/.01	1



https://cloud.google.com/compute/pricing

https://cloud.google.com/storage/pricing#pricing-example-simple

Mathematical Formulation

Inputs:

 $v_{a,f}^{s,m}$: Offered traffic of application profile a, between node pair (s,m), destined for node f (f in core or metro)

 $\theta_{a,f,m}:$ Residual latency budget of traffic destined for core node f of application profile $a,\!{\rm processed}$ at node m

 $A = A_p \cup A_s \cup A_{sp} \cup A_n$

 A_s : Set of all application profiles requiring storage only A_p : Set of all application profiles requiring processing only A_{sp} : Set of all application profiles requiring processing and storage A_n : Set of all application profiles requiring neither processing nor storage



Inputs:

 N_c : set of nodes directly attached to core network N_g : set of nodes that generate traffic (sources of data)g N_{DC} : set of data center nodes $N = N_c \cup N_g \cup N_{DC}$ $N_p = N_g \cup N_{DC}$: Set of all nodes capable of processing $N_s = N_g \cup N_{DC}$: Set of all nodes capable of storage $N_l = N_g$ Set of local nodes capable of processing (excluding DC)

- F_c : Set of distant core nodes
- $\eta_{s,d}$: set of all admissible paths between node pair (s,d)
- $\delta_k^{s,d}$: Total prop delay on the k^{th} adm path between node pair (s,d)
- $\zeta_k^{s,d}$: Total trans delay on the k^{th} adm path between node pair (s,d)
- U_m : processing capacity of node m, in CPUs
- E_f : storage capacity of node f, in Gbit



Variables:

 $A_p: x_{a,f}^{s,m} = 1$ if traffic of app profile a, destined for node f, generated at source node s, is processed at node m

 $A_s: x_{a,f}^{s,m} = 1$ if traffic of app profile a, generated at node s, is stored at node f, m = f

 $A_{sp}: x_{a,f}^{s,m} = 1$ if traffic of app profile a, generated at source node s, is processed at node m and stored at node f

 $A_p, A_{sp}: r_{a,k,f}^{s,m} = 1$ if traffic of application profile **a** is routed over the k^{th} admissible path between node pair (s, m), destined for node f

 $A_s: r_{a,k,f}^{s,m} = 1$ if traffic of application profile **a** is routed over the k^{th} admissible path between node pair (s,m), m = f

 $A_n: r_{a,k,f}^{s,m} = 1$ if traffic of application profile *a* is routed over the k^{th} admissible path between node pair (s, m), internal: m = f, external: $m \in N_c$



Variables:

 $A_p, A_{sp}, A_s: r_{a,k,f}^{s,m} = 1$ if traffic of application profile a is routed over the k^{th} admissible path between node pair $(s, m), m \in N_p, A_s: m \in N_s$ $A_p, A_{sp}: r_{a,k,f}^{\prime s,m} = 1$ if traffic of application profile a is routed over the k^{th} admissible path between node pair $(m, f), m \in N_p, f \in N_g, A_{sp}: f \in N_s$ $A_p, A_{sp}: r_{a,k,f}^{\prime \prime s,m,d} = 1$ if traffic of application profile a is routed over the k^{th} admissible path between node pair (m, d), destined for core node $f, m \in N_p, f \in F_c, d \in N_c$



Objective Function:

$$min(Cost_{p} + Cost_{s} + Cost_{u} + Cost_{d} + Cost_{cap})$$

$$Cost_{p} = \sum_{m \in N_{p}} \gamma_{m} \sum_{a \in A_{p} \cup A_{sp}} \alpha_{a} \sum_{s \in N_{g}} \sum_{f \in N \cup F_{c}} x_{a,f}^{s,m} v_{a,f}^{s,m} \operatorname{Processing}$$

$$Cost_{s} = \sum_{a \in A_{s}} \Delta_{a} \sum_{m = f \in N_{p}} \nu_{f} \sum_{s \in N_{g}} x_{a,f}^{s,m} v_{a,f}^{s,m} + \sum_{a \in A_{sp}} \Delta_{a} \beta_{a} \sum_{f \in N_{p}} \nu_{f} \sum_{s \in N_{g}} \sum_{m \in N_{p}} x_{a,f}^{s,m} v_{a,f}^{s,m}$$
source to storage proc to storage, source to proc/storage Storage
$$Cost_{d} = \epsilon_{down} \Big[\sum_{a \in A_{p}} \beta_{a} \sum_{s \in N_{g}} \sum_{f \in N_{g}} \sum_{m \in N_{DC}} x_{a,f}^{s,m} v_{a,f}^{s,m} + \sum_{a \in A_{sp}} \beta_{a} \sum_{s \in N_{g}} \sum_{f \in N_{l}} \sum_{m \in N_{DC}} x_{a,f}^{s,m} v_{a,f}^{s,m} + \sum_{a \in A_{sp}} \beta_{a} \sum_{s \in N_{g}} \sum_{f \in N_{l}} \sum_{m \in N_{DC}} x_{a,f}^{s,m} v_{a,f}^{s,m} \Big]$$
Downstream



Objective Function (cont.):

$$Cost_{u} = \epsilon_{up} \left[\sum_{a \in A_{p}} \beta_{a} \sum_{m \in N_{l}} \sum_{s \in N_{g}} \sum_{f \in F_{c}} x_{a,f}^{s,m} v_{a,f}^{s,m} + \sum_{a \in A_{sp}} \beta_{a} \sum_{m \in N_{l}} \sum_{s \in N_{g}} \sum_{f \in N_{DC}} x_{a,f}^{s,m} v_{a,f}^{s,m} + \sum_{local proc, storage at DC} \sum_{local proc, storage at DC} \sum_{a \in A_{n}} \sum_{m \in N_{c}} \sum_{s \in N_{g}} \sum_{f \in F_{c}} v_{a,f}^{s,m} + \sum_{a \in A_{p}} \sum_{s \in N_{g}} \sum_{f \in N \cup F_{c}} x_{a,f}^{s,m} v_{a,f}^{s,m} + \sum_{x \in A_{p}} \sum_{s \in N_{g}} \sum_{f \in N \cup F_{c}} x_{a,f}^{s,m} v_{a,f}^{s,m} + \sum_{a \in A_{p}} \sum_{s \in N_{g}} \sum_{f \in N \cup F_{c}} x_{a,f}^{s,m} v_{a,f}^{s,m} + \sum_{a \in A_{sp}} \beta_{a} \sum_{s \in N_{g}} \sum_{f \in N_{l}} \sum_{m \in N_{DC}} x_{a,f}^{s,m} v_{a,f}^{s,m} + \sum_{a \in A_{s}} \sum_{s \in N_{g}} \sum_{m = f \in DC} x_{a,f}^{s,m} v_{a,f}^{s,m} \right]$$
Upstream Proc at DC, stored in metro



Objective Function (cont.):

$$\sum_{a \in A_n \cup A_s} \sum_{s \in N_g} \left[\sum_{m=f \in N_s} \sum_{k \in R_{i,j}} r_{a,k,f}^{s,m} v_{a,f}^{s,m} + \sum_{f \in F_c} \sum_{m \in N_c} \sum_{k \in R_{i,j}} r_{a,k,f}^{s,m} v_{a,f}^{s,m} \right] = C_1$$

$$\sum_{a \in A_p \cup A_{sp}} \sum_{s \in N_g} \sum_{m \in N_p} \sum_{f \in N \cup F_c} \sum_{k \in R_{i,j}} r_{a,k,f}^{s,m} v_{a,f}^{s,m} = C_2$$

$$\sum_{a \in A_p \cup A_{sp}} \beta_a \sum_{s \in N_g} \sum_{f \in N_g \cup N_s} \sum_{m \in N_p} \sum_{k \in R_{i,j}} r_{a,k,f}^{\prime s,m} v_{a,f}^{s,m} = C_3$$

$$\sum_{a \in A_p} \beta_a \sum_{s \in N_g} \sum_{f \in F_c} \sum_{m \in N_g} \sum_{d \in N_c} \sum_{k \in R_{i,j}} r_{a,k,f}^{\prime \prime s,m,d} v_{a,f}^{s,m} = C_4$$

$$\Lambda \sum_{(i,j) \in L_m} C_1 + C_2 + C_3 + C_4 = Cost_{cap}$$
Capacity



Constraints:

$$\sum_{m \in N_p} x_{a,f}^{s,m} = 1, \forall \ (a \in A_p, s \in N_g, f \in N \cup F_c)$$

$$\sum_{f=m\in N_s} x_{a,f}^{s,m} = 1, \forall \ (a \in A_s, s \in N_g)$$

$$\sum_{m \in N_p} \sum_{f \in N_s} x_{a,f}^{s,m} = 1, \forall \ (a \in A_{sp}, s \in N_g)$$

$$\sum_{a \in A_p} \alpha_a \sum_{s \in N_g} \sum_{f \in N \cup F_c} x_{a,f}^{s,m} v_{a,f}^{s,m} \le U_m \quad \forall m \in N_p \qquad \text{Processing}$$

$$\sum_{a \in A_s} \Delta_a \sum_{s \in N_g} x_{a,f}^{s,m} v_{a,f}^{s,m} + \sum_{a \in A_{sp}} \Delta_a \beta_a \sum_{s \in N_g} \sum_{m \in N_p} x_{a,f}^{s,m} v_{a,f}^{s,m} \le E_f, \ \forall f \in N_s$$

Storage



Constraints (cont.): Solenoidality

$$\sum_{k} r_{a,k,f}^{s,m} = 1, \forall (a \in A_n, s, f \in N_g, m = f)$$

$$\sum_{m \in N_c} \sum_{k} r_{a,k,f}^{s,m} = 1, \forall (a \in A_n, s \in N_g, f \in F_c)$$

$$\sum_{k} r_{a,k,f}^{s,m} = x_{a,f}^{s,m}, \forall (a \in A_p \cup A_{sp} \cup A_s, s \in N_g, m \in N_p, f \in N \cup F_c)$$

$$\sum_{k} r_{a,k,f}^{\prime s,m} = x_{a,f}^{s,m}, \forall (a \in A_p \cup A_{sp}, s \in N_g, m \in N_p, f \in N_s \cup N_g)$$

$$\sum_{k} \sum_{k} r_{a,k,f}^{\prime \prime s,m,d} = x_{a,f}^{s,m}, \forall (a \in A_p, s \in N_g, m \in N_g, f \in F_c)$$



source to dest

Constraints (cont.): Latency

$$\begin{split} \sum_{k \in \eta_{s,m}} r_{a,k,f}^{s,m}(\delta_k^{s,m} + \zeta_k^{s,m}) + \sum_{d \in N_c} \sum_{k \in \eta_{s,d}} r_{a,k,f}^{s,d}(\delta_k^{s,d} + \zeta_k^{s,d}) &\leq \theta_{a,f} \\ \forall (a \in A_n, s, m \in N_g, f \in N \cup F_c) \\ \gamma_m &= \alpha_a \kappa_a x_{a,f}^{s,m} \tau_m \longleftarrow \text{Processing delay at node m} \\ \sum_{m \in N_p} \left[\sum_{k \in \eta_{s,m}} r_{a,k,f}^{s,m}(\delta_k^{s,m} + \zeta_k^{s,m}) + \gamma_m + \sum_{k' \in \eta_{m,f}} r_{a,k',f}^{\prime s,m}(\delta_{k'}^{m,f} + \zeta_{k'}^{m,f}) \right] \leq \Theta_a \\ \forall (A \in A_p, s, f \in N_g) \\ \sum_{m \in N_p} \left[\sum_{k \in \eta_{s,m}} r_{a,k,f}^{s,m}(\delta_k^{s,m} + \zeta_k^{s,m}) + \gamma_m + \sum_{m \in N_p} x_{a,f}^{s,m} \theta_{a,f,m} \ \forall (A \in A_p, s \in N_g, f \in F_c) \right] \\ \end{bmatrix}$$



Constraints (cont.): Latency

$$\sum_{f \in N_s} \sum_{m \in N_p} \left[\sum_{k \in \eta_{s,m}} r_{a,k,f}^{s,m} (\delta_k^{s,m} + \zeta_k^{s,m}) + \gamma_m + \sum_{k' \in \eta_{m,f}} r_{a,k',f}^{\prime s,m} (\delta_{k'}^{m,f} + \zeta_{k'}^{m,f}) \right] \le \Theta_a$$

 $\forall (A \in A_{sp} \cup A_s, s \in N_q)$

Processing delay: $\gamma_m = \alpha_a \kappa_a x_{a,f}^{s,m} \tau_m$

$$sec = \left(\frac{CPU}{Mbps}\right)(Mb)\left(\frac{1}{CPU}\right)$$

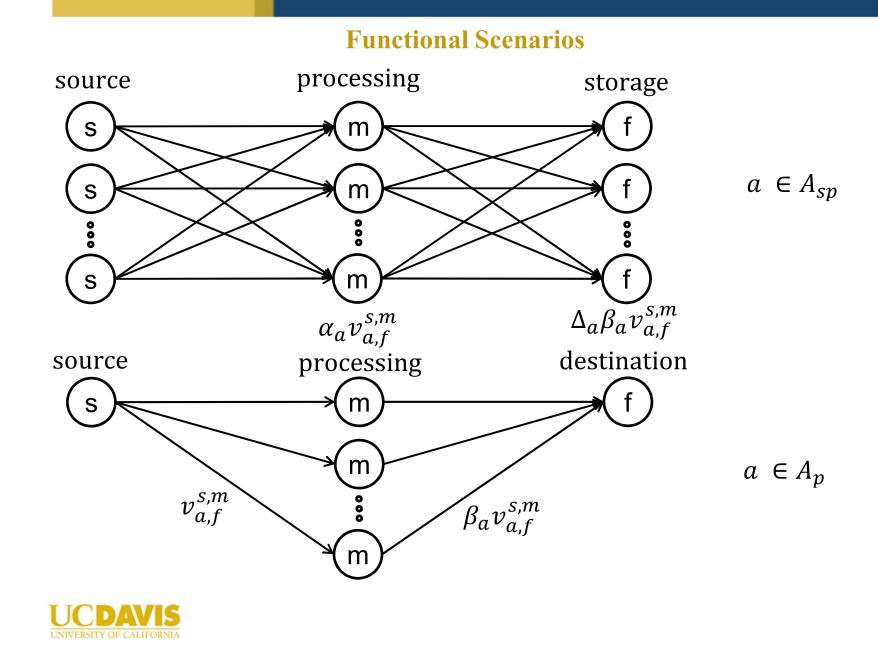
Processing Capacity: $U_m = \alpha_a x_{a,f}^{s,m} v_{a,f}^{s,m}$

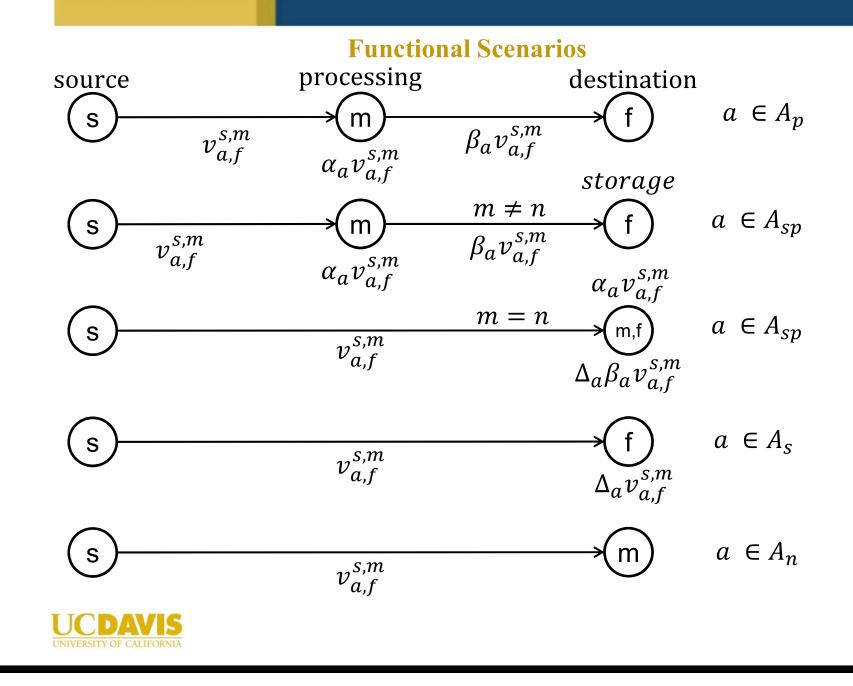
$$CPU = \left(\frac{CPU}{Mbps}\right)(Mbps)$$

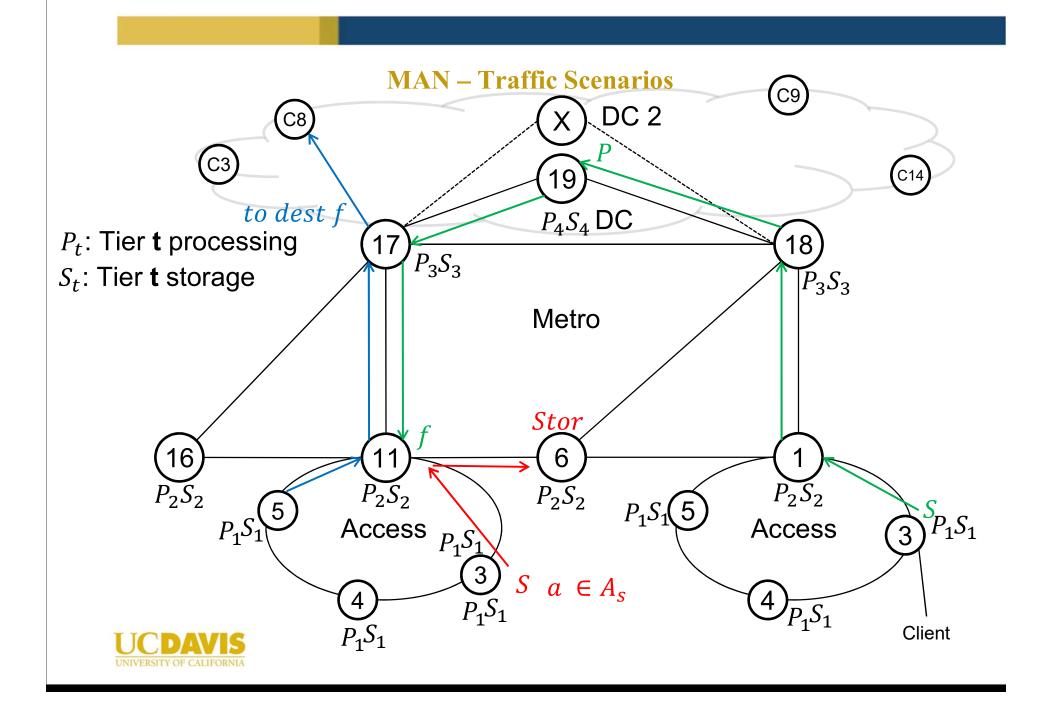
Storage Capacity: $E_f = \Delta_a x_{a,f}^{s,m} v_{a,f}^{s,m}, \beta_a$ if necessary

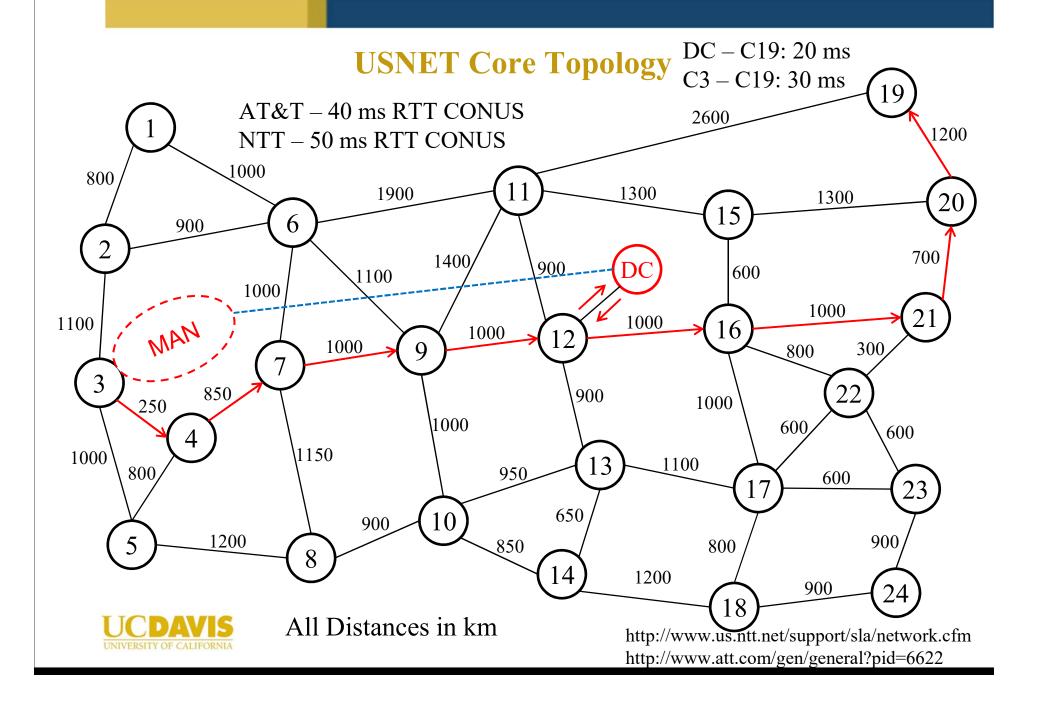


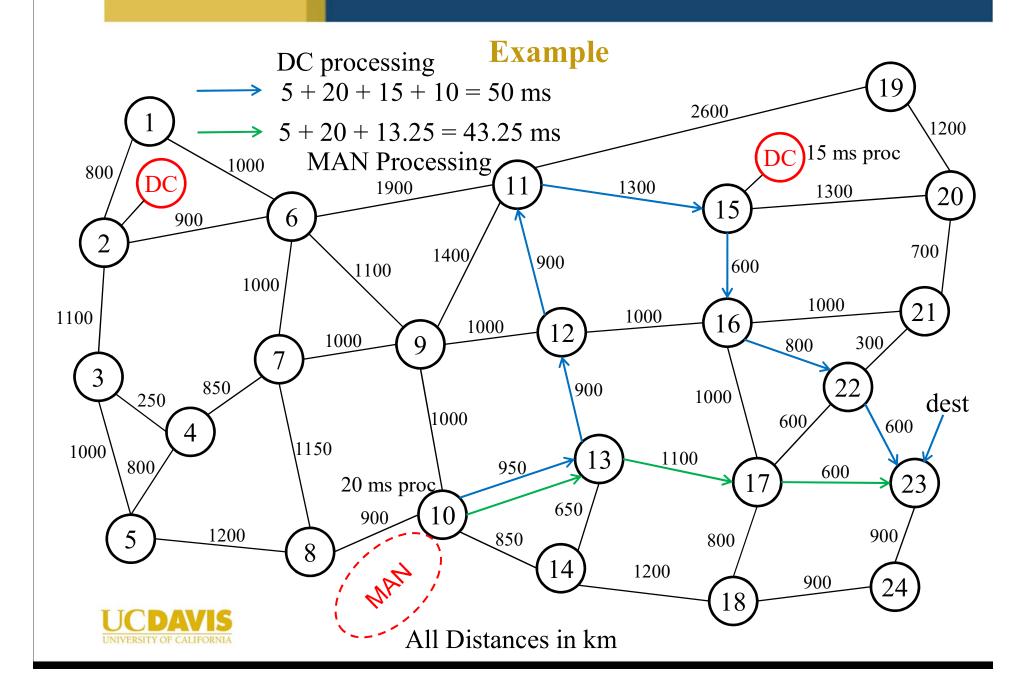
$$GB = (sec) \left(\frac{Mbit}{sec}\right) \left(\frac{GB}{Mbit}\right)$$

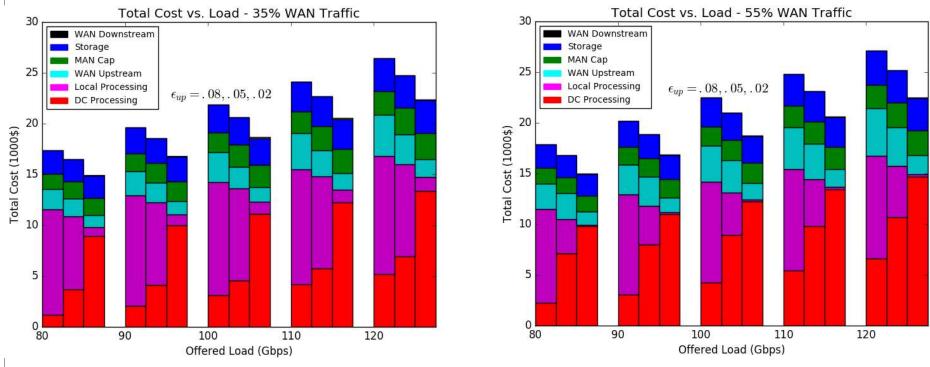






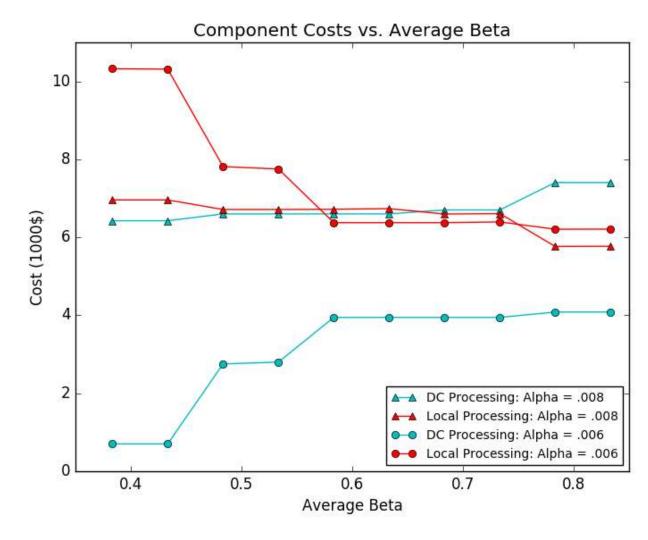






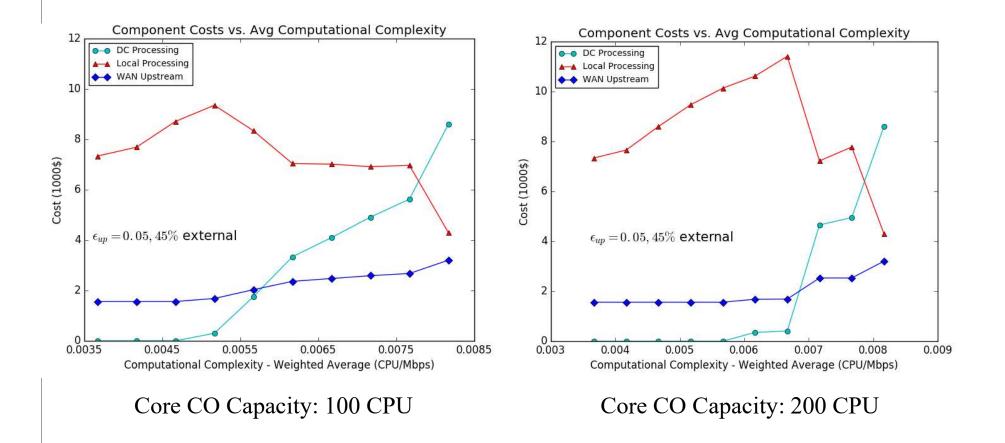
- WAN upstream increases slightly with more external traffic
- At lower WAN upstream per unit costs, DC processing almost 100% of
- total processing costs



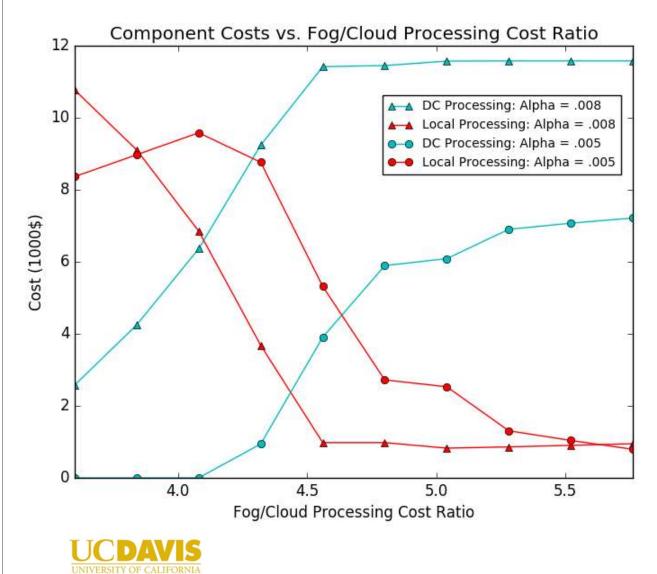


With average $\alpha = 0.006$, local and DC processing begin to converge with increasing β ; with average $\alpha = 0.008$, costs are similar at smaller β , begin to slightly diverge with increasing β .

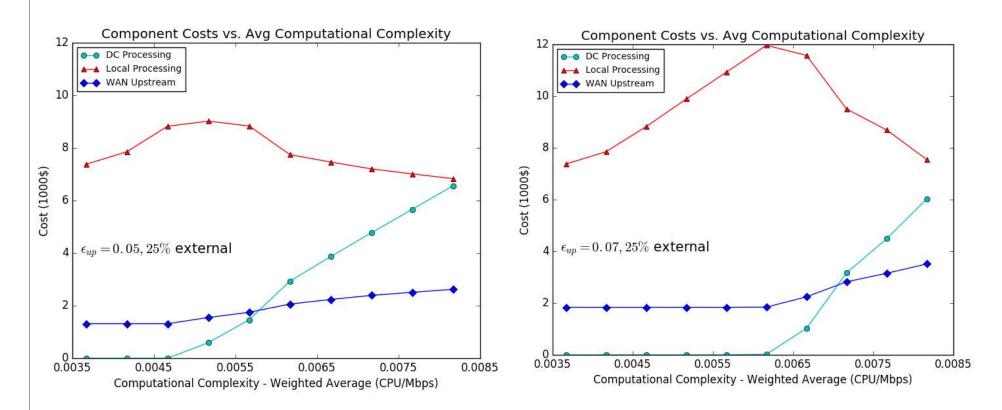






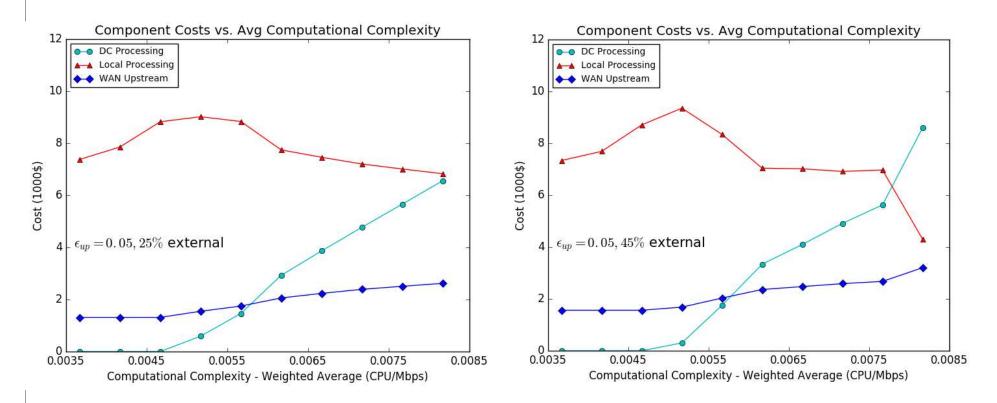


With greater average α , local and DC processing costs intersect and reach steady state at lower fog/cloud cost ratios.



More expensive WAN bandwidth causes a higher peak and sharper decline in local processing with increasing computational complexity





External traffic is more affected by latency constraints, and thus have more abrupt changes in processing costs from fog to cloud or vice versa



Ongoing Work

- Reconfigure core network: multiple DCs, with strategic placement such that latency constraints have greater impact in processing/storage locations
- Dynamic Simulation:
 - Apply static optimal solution and conduct performance evaluation
 - Poisson, Power Law, and periodic offered traffic
- Extension: Storage locations can be viewed as potential multicast sources that are accessible from clients distributed across the world
 - Can extend problem to better decide storage locations or possibly move storage analysis from metro to distributed across core

