

# Virtual-Pod-Assisted Routing and Resource Assignment in Elastic All-Optical Intra-Datacenter Networks

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Speaker: Lin Wang

Peng, L. et. al., “Virtual-Pod-Assisted Routing and Resource Assignment in Elastic All-Optical Intra-Datacenter Networks,” IEEE Access, 5, pp.406-420.



**Motivations**



**ILP Model**



**Dynamic spectrum/IT resource assignment**



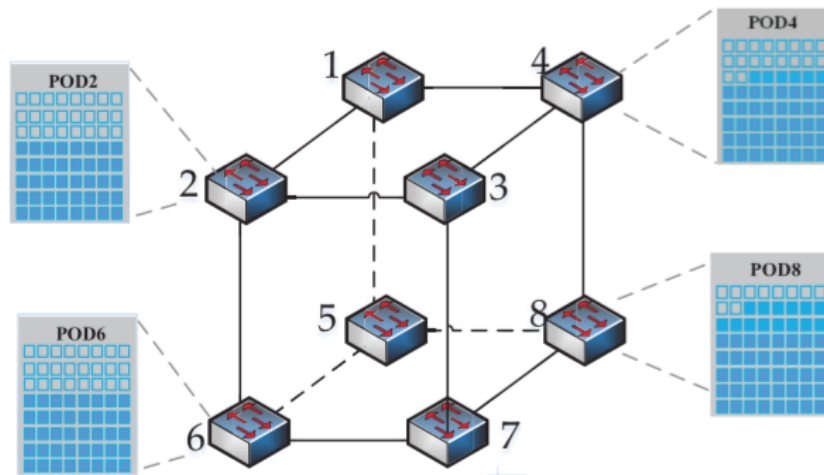
**Simulation Results**

## Motivation

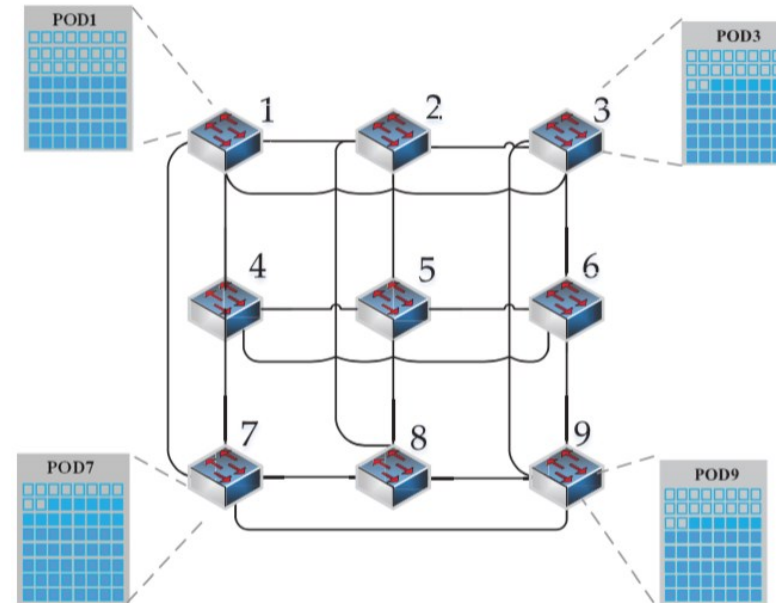
- **The service requests of intra-datacenter networks are different from that of traditional transport networks**
  - Traffic in traditional networks is between dedicated node pairs that only require sufficient transmission bandwidth
  - Intra-DCN service requests, require IT resources and transmission bandwidth
  - Any intra-DCN node that can provide the required IT resources can serve as a destination node (i.e., anycast)
- **Routing and spectrum/IT resource assignment (RSIA)**

## Intra-DCN architectures

- N-cube topology
- Torus topology



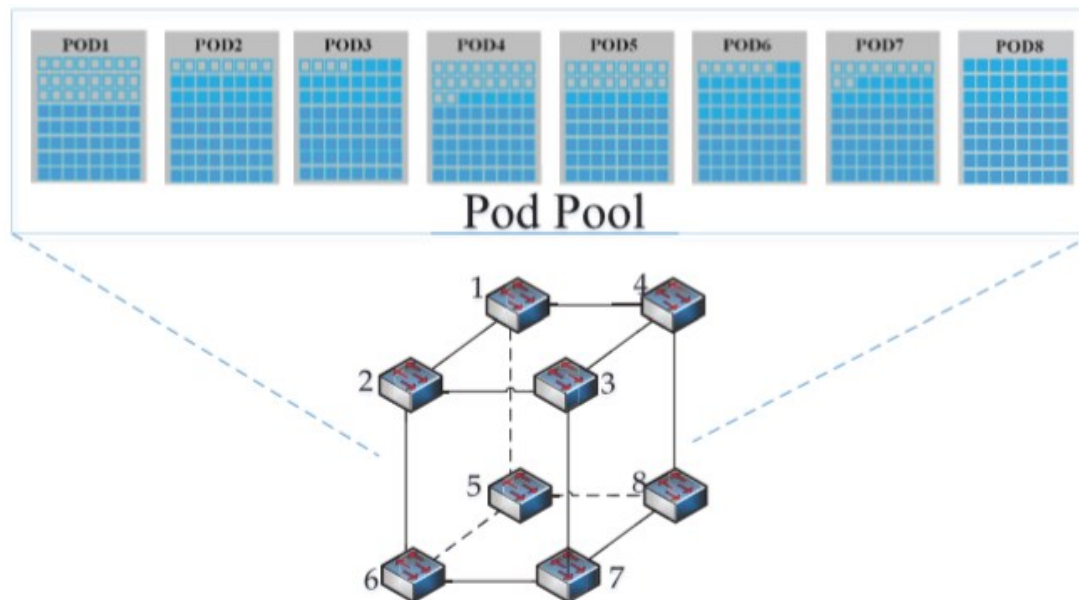
A 3-cube elastic intra-DCN architecture.



A 3-by-3 Torus elastic intra-DCN architecture.

## Virtual-pod pool intra-DCN architectures

- Flexible number of destination nodes
- Destination node is not preset
- IT units of different pods can be shared





**Motivations**



**ILP Model**



**Dynamic spectrum/IT resource assignment**



**Simulation Results**

# **ILP MODEL FOR STATIC ROUTING AND SPECTRUM/IT ASSIGNMENT (RSIA)**

- **ANYCAST ILP MODEL FOR INTRA-DCN STATIC RSIA**
- **UNICAST ILP MODEL FOR INTRA-DCN STATIC RSIA**

# ANYCAST ILP MODEL FOR INTRA-DCN STATIC RSIA

- **Given**
  - $V$  : Set of intra-DCN nodes.
  - $L$  : Set of intra-DCN links.
  - $R$ : Set of service request indices,  $1, 2, \dots, N$ .
  - Service-request (SR) is represented as SR (SRC, BW, IT)
  - $LKi$  : Set of links that start or end at node  $i$ .
- **Objective**
  - Minimize maximum number of required spectrum slots, and the maximum number of required IT units of all the destination nodes.

Minimize  $F+I$



# ANYCAST ILP MODEL FOR INTRA-DCN STATIC RSIA

- **Parameters**
- $SRC_i$ : Source node of service request  $i$ .
- $BW_i$ : Number of spectrum slots required by service request  $i$ .
- $IT_i$ : Number of IT units required by service request  $i$ .
- $F_{max}$ : Total number of required spectrum slots by all the intra-DCN service requests. It is calculated as the sum of the required spectrum slots of all the service requests.
- $G$ : Guard band required in units of spectrum slot unit between two spectrally neighboring elastic optical channels.

# ANYCAST ILP MODEL FOR INTRA-DCN

## STATIC RSIA

- **Variables**

- $PLmin$ : A binary variable. The value is equal to 1 if the lightpath for service request  $i$  traverses physical link  $mn$ ; zero, otherwise.
- $PNmi$ : A binary variable. The value is equal to 1 if the lightpath for service request  $i$  traverses physical node  $m$ ; zero, otherwise.
- $FNmi$ : A binary variable. The value is equal to 1 if  $m$  is the final physical node, i.e., destination node, traversed by the lightpath for service request  $i$ ; zero, otherwise.
- $fi$ : Starting spectrum slot index of service request  $i$ .
- $\beta_{i,j}$ : A binary variable that takes value one if  $fi < fj$ ; zero, otherwise.
- $F$ : Maximum index of required spectrum slots among all the fiber links of the entire intra-DCN.
- $I$ : Maximum number of required IT units among all the destination nodes of the entire intra-DCN.

# ANYCAST ILP MODEL FOR INTRA-DCN STATIC RSIA

## • Constraints

$$\sum_{mn \in LK_{SRC_i}} PL_{mn}^i = 1, \quad \forall i \in R \quad (1)$$

$$\sum_{m \in N} FN_m^i = 1, \quad \forall i \in R \quad (2)$$

$$FN_m^i \leq PN_m^i, \quad \forall i \in R, \forall m \in V \quad (3)$$

$$\begin{aligned} \sum_{mn \in LK_w} PL_{mn}^i &= 2PN_w^i - FN_w^i, \\ &\forall i \in R, \quad w! = SRC_i \end{aligned} \quad (4)$$

$$\begin{aligned} PN_m^i + PN_n^i &\geq 2 * PL_{mn}^i, \quad \forall i \in R, \forall m, n \in V, \\ &\forall mn \in L \end{aligned} \quad (5)$$

$$F \leq F_{max} \quad (6)$$

$$F \geq f_i + BW_i + G, \quad \forall i \in R \quad (7)$$

$$F \geq \sum_{i \in R} PL_{mn}^i * BW_i, \quad \forall mn \in L \quad (8)$$

$$\beta_{i,j} + \beta_{j,i} = 1, \quad \forall i, j \in R \quad (9)$$

$$\begin{aligned} f_i + BW_i + G - f_j &\leq F_{max}(1 - \beta_{i,j} + 2 - PL_{mn}^i \\ &\quad - PL_{mn}^j), \quad \forall i, j \in R, \forall mn \in L \end{aligned} \quad (10)$$

$$\sum_i FN_m^i * IT_i \leq I, \quad \forall i \in R, \forall m \in V \quad (11)$$

$$IT_i \leq I, \quad \forall i \in R \quad (12)$$

# UNICAST ILP MODEL FOR INTRA-DCN STATIC RSIA

- **Given**
  - $V$  : Set of intra-DCN nodes.
  - $L$  : Set of intra-DCN links.
  - $SD$  : Set of intra-DCN source-destination node pairs.
  - $LKi$  : Set of links that start or end at node  $i$ .
- **Objective**
  - Minimize maximum number of required spectrum slots, and the maximum number of required IT units of all the destination nodes.

Minimize  $F+I$

# UNICAST ILP MODEL FOR INTRA-DCN STATIC RSIA

- **Parameters**
- $BW_i$ : Number of spectrum slots required by service request  $i$ .
- $IT_{sd}$ : Number of IT units required by node pair  $sd$ .
- $F_{max}$ : Total number of required spectrum slots by all the intra-DCN service requests. It is calculated as the sum of the required spectrum slots of all the service requests.
- $G$ : Guard band required in units of spectrum slot unit between two spectrally neighboring elastic optical channels.

# UNICAST ILP MODEL FOR INTRA-DCN STATIC RSIA

- **Variables**

- $PL_{sd}$  : A binary variable. The value is equal to 1 if the mn lightpath for node pair  $sd$  traverses physical link  $mn$ ; zero, otherwise.
- $PN_{sd}$ : A binary variable. The value is equal to 1 if the lightpath for node pair  $sd$  traverses physical node  $m$ ; zero, otherwise.
- $f_{sd}$ : Starting spectrum-slot index for a service request between node pair  $sd$ .
- $\beta_{sd1, sd2}$  : A binary variable that takes value one if  $f_{sd1} < f_{sd2}$ ; zero, otherwise.
- $F$ : Maximum index of required spectrum slots among all the fiber links of the entire intra-DCN.
- $I$ : Maximum number of required IT units among all the destination nodes of the entire intra-DCN.

# UNICAST ILP MODEL FOR INTRA-DCN STATIC RSIA

## • Constraints

$$\sum_{mn \in LK_s} PL_{mn}^{sd} = 1, \quad \forall sd \in SD \quad (13)$$

$$\sum_{mn \in LK_d} PL_{mn}^{sd} = 1, \quad \forall sd \in SD \quad (14)$$

$$\sum_{mn \in LK_w} PL_{mn}^{sd} = 2PN_w^{sd}, \quad \forall sd \in SD, w! = s, d \quad (15)$$

$$PN_m^{sd} + PN_n^{sd} \geq 2 * PL_{mn}^{sd}, \quad \forall sd \in SD, \forall m, n \in V, \\ \forall mn \in L \quad (16)$$

$$F \leq F_{max} \quad (17)$$

$$F \geq f_{sd} + BW_{sd} + G, \quad \forall sd \in SD \quad (18)$$

$$F \geq \sum_{sd \in SD} PL_{mn}^{sd} * BW_{sd}, \quad \forall mn \in L \quad (19)$$

$$\beta_{sd1, sd2} + \beta_{sd2, sd1} = 1, \quad \forall sd \in SD \quad (20)$$

$$f_{sd1} + BW_{sd1} + G - f_{sd2} \\ \leq F_{max}(1 - \beta_{sd1, sd2} + 2 - PL_{mn}^{sd} - PL_{mn}^{sd}), \\ \forall sd \in SD, \quad \forall mn \in L \quad (21)$$

$$\sum_{s \in V} IT_{sd} \leq I, \quad \forall sd \in SD \quad (22)$$

## Complexity comparison for two ILP models

**TABLE 1.** Complexity comparison for a 3-Cube and a 3-by-3 Torus intra-DCN topologies based on the actual numbers of variables and Constraints given by Gurobi ILP solver. No. of service requests = 12.

Model Name		Rows(Variables)	Columns(Constraints)
3-Cube	<i>Anycast</i>	428	2108
	<i>Unicast</i>	506	2086
3*3 Torus	<i>Anycast</i>	578	3003
	<i>Unicast</i>	482	2862

**TABLE 2.** Results comparison for anycast ILP model and unicast ILP model. SRs = 12 means the number of service requests is 12.

Model Name	SRs = 12		SRs = 16		SRs = 20	
	<i>F</i>	<i>I</i>	<i>F</i>	<i>I</i>	<i>F</i>	<i>I</i>
<i>3-Cube-Anycast</i>	209	76	209	76	289	76
<i>3-Cube-Unicast</i>	209	76	209	76	289	76
<i>3 * 3 Torus-Anycast</i>	150	40	189	52	248	58
<i>3 * 3 Torus-Unicast</i>	257	114	277	118	405	118





**Motivations**



**ILP Model**



**Dynamic spectrum/IT resource assignment**

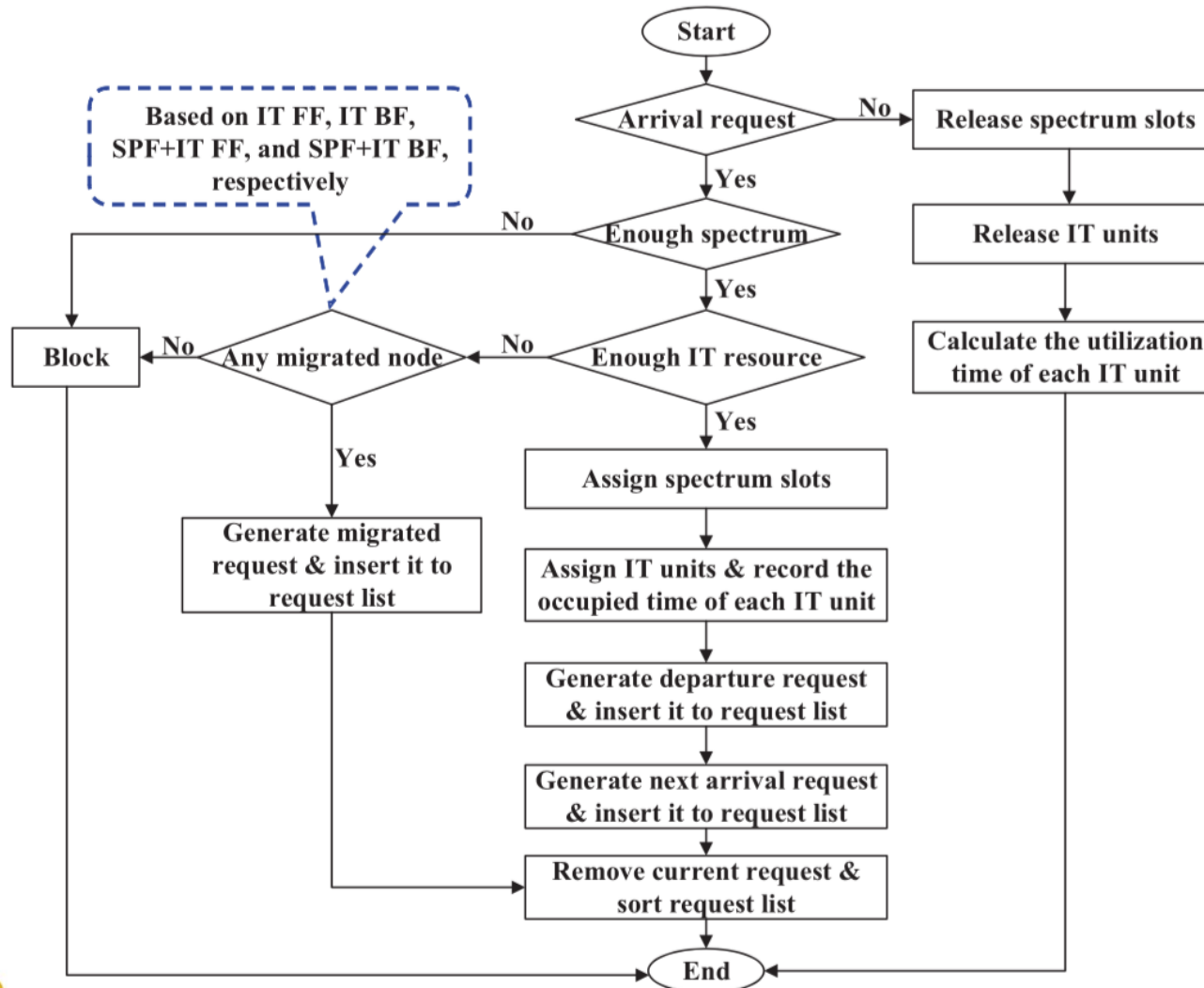


**Simulation Results**

# V-POD-ASSISTED ALGORITHMS FOR DYNAMIC RSIA

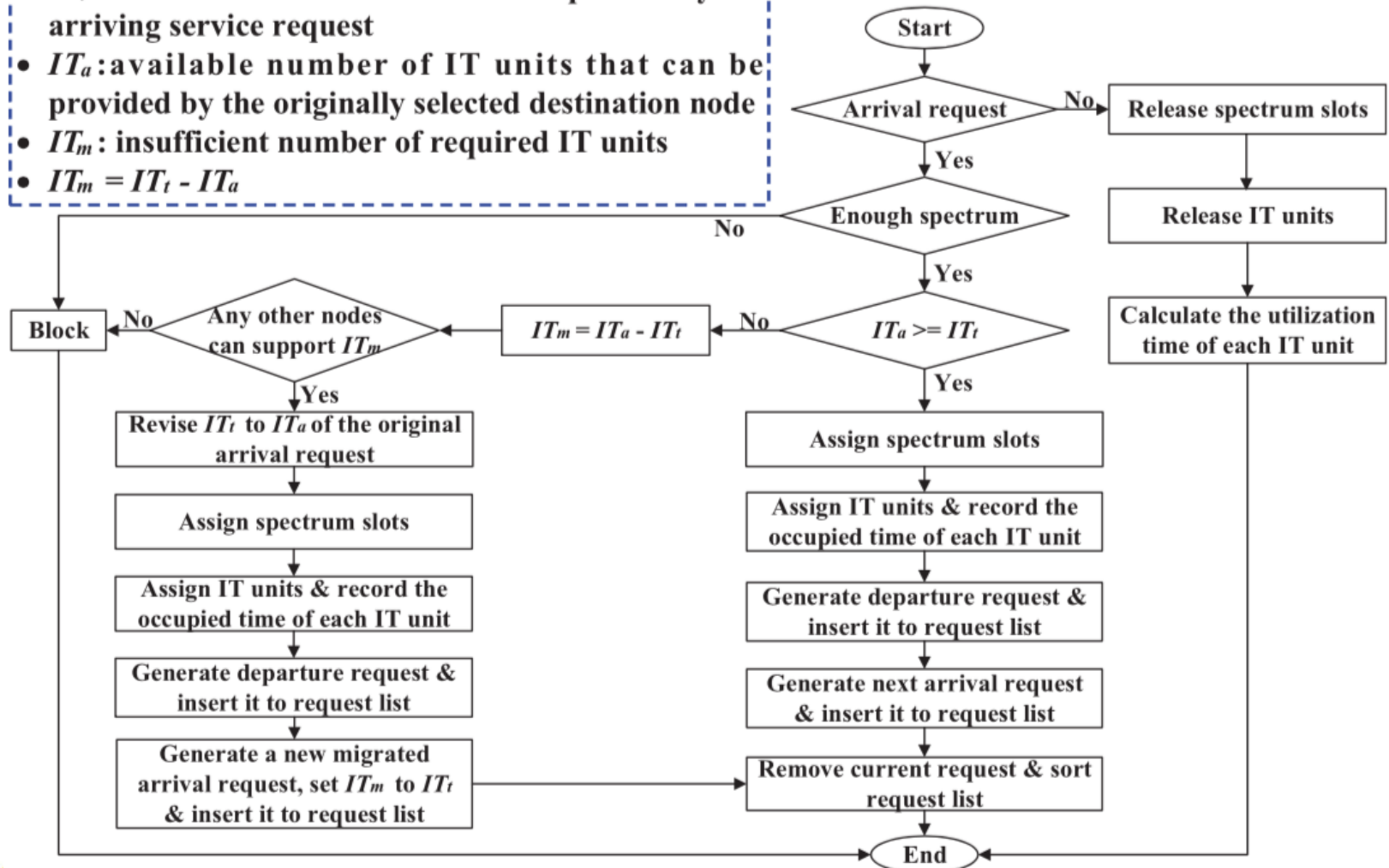
- **Full migration**
- **Partial migration**

# Full Migration Algorithms FOR DYNAMIC RSIA



# Partial Migration Algorithms FOR DYNAMIC RSIA

- $IT_t$ : total number of IT units required by an arriving service request
- $IT_a$ : available number of IT units that can be provided by the originally selected destination node
- $IT_m$ : insufficient number of required IT units
- $IT_m = IT_t - IT_a$





**Motivations**



**ILP Model**



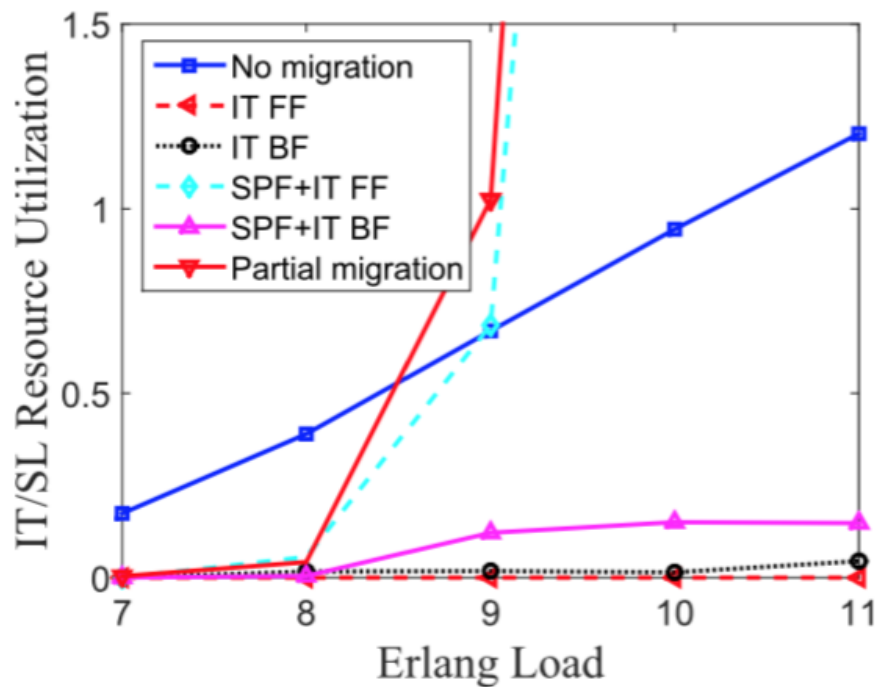
**Dynamic spectrum/IT resource assignment**



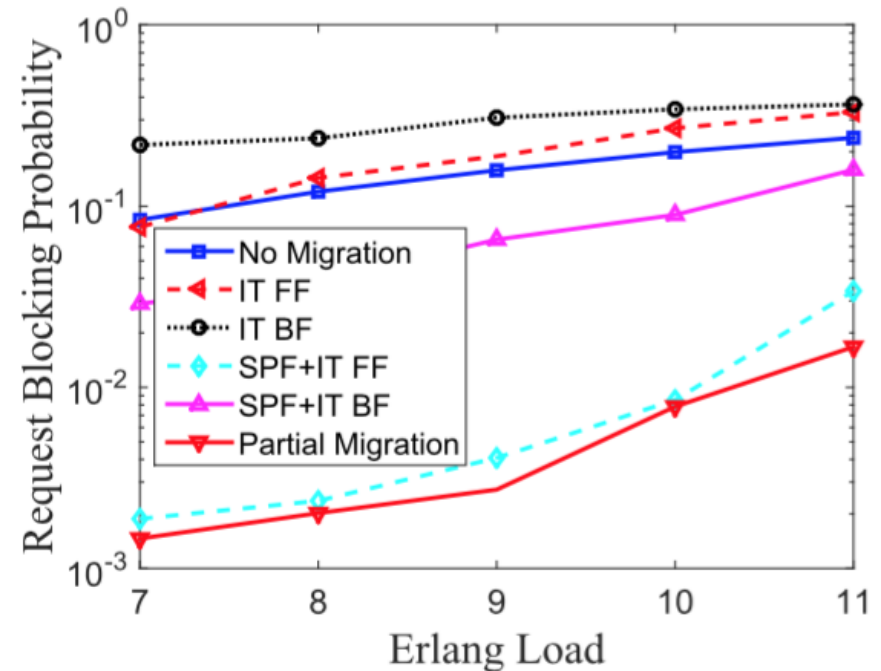
**Simulation Results**

# Simulation Results for A 4-cube Intra-DCN

- 4-cube intra-DCN
- 16 pods and 32 optical fiber links
- 400 IT units per pod
- 5 GHz spectrum slot



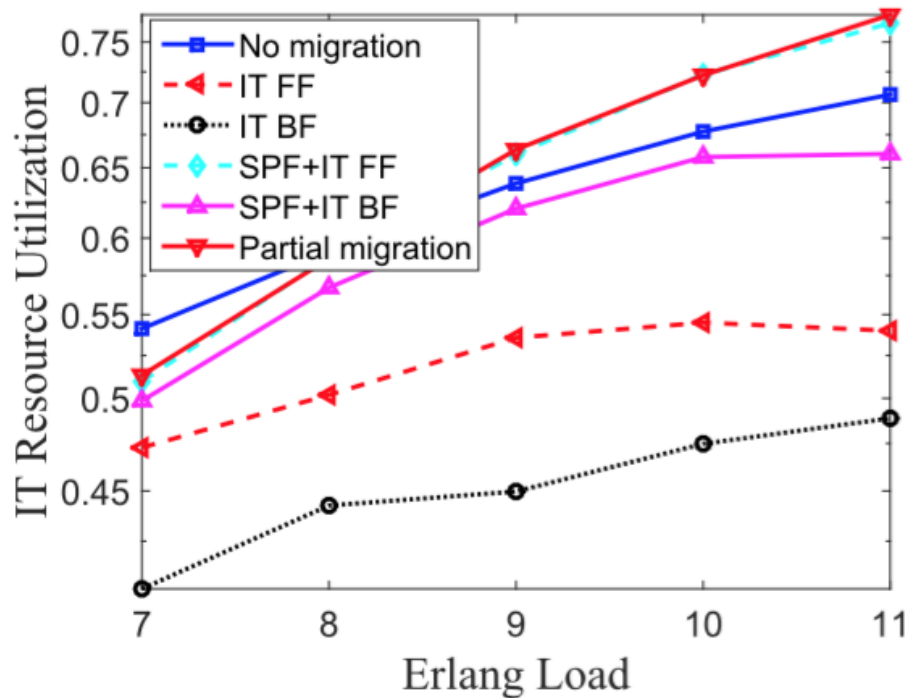
Loss ratio of IT units to spectrum slots.



Service-request blocking probability.

## Simulation Results for A 4-cube Intra-DCN

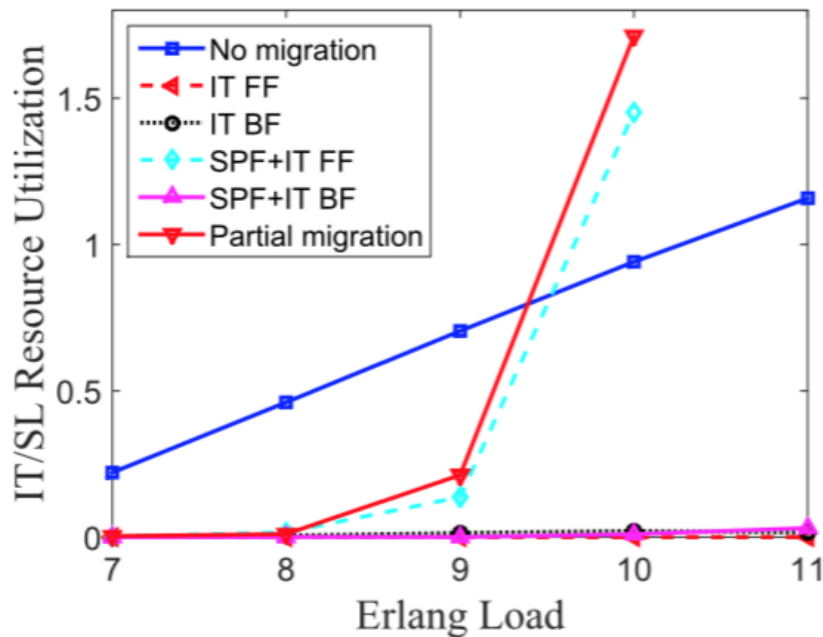
- 4-cube intra-DCN
- 16 pods and 32 optical fiber links
- 400 IT units per pod
- 5 GHz spectrum slot



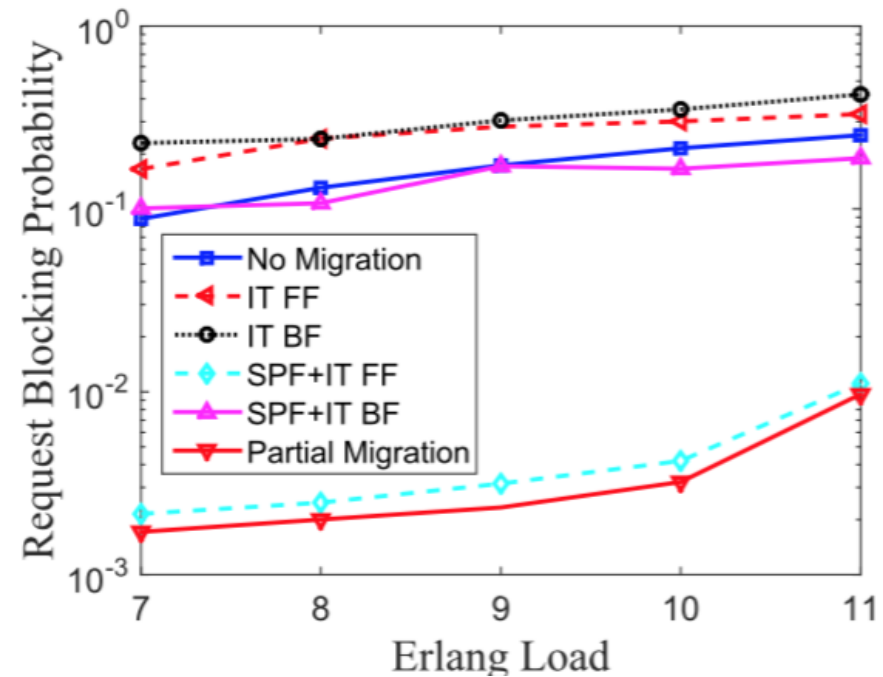
IT resource utilization.

# Simulation Results for A 4-by-4 Torus Intra-DCN

- 4-by-4 torus intra-DCN
- 16 pods and 32 optical fiber links
- 200 IT units per pod
- 5 GHz spectrum slot



Loss ratio of IT units to spectrum slots

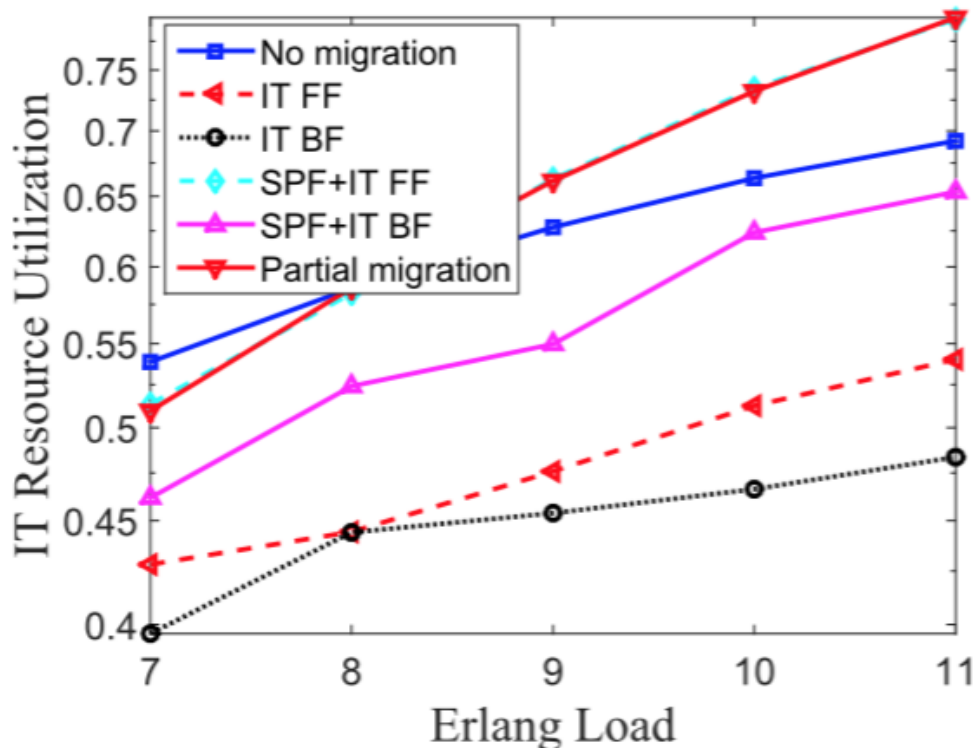


Service-request blocking probability



## Simulation Results for A 4-by-4 Torus Intra-DCN

- 4-by-4 torus intra-DCN
- 16 pods and 32 optical fiber links
- 200 IT units per pod
- 5 GHz spectrum slot





Thank You !

- [amlwang@ucdavis.edu](mailto:amlwang@ucdavis.edu)